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## Unification of Model-Checking, Scheduling, and Code Synthesis:

From UPPAAL to TIMES

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## OUTLINE

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- A Brief Introduction
  - Motivation ... what are the problems to solve
  - CTL, LTL and basic model-checking algorithms
- Timed Systems
  - Timed automata and verification problems
  - UPPAAL tutorial: data structures & algorithms
  - TIMES: [schedulability analysis using timed automata](#)



- Recent Work
  - The multicore timing analysis problems
  - Some solutions: WCET analysis and multiprocessor scheduling

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## "Who is Who" in Real Time Systems

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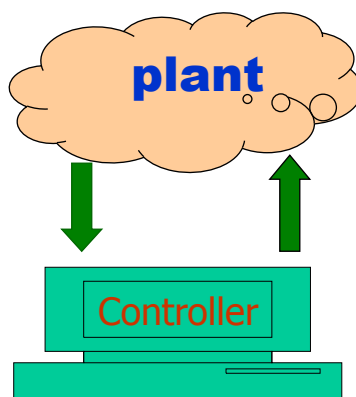
- Real Time Scheduling [RTSS ...]
  - Task models, Schedulability analysis
  - Real time operating systems
- Automata/logic-based methods [CAV,TACAS ...]
  - FSM, PetriNets, Statecharts, Timed Automata
  - Modelling, Model checking ...
- (RT) Programming Languages [...]
  - Esterel, Signal, Lustre, Ada ...
- ... ..

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## The Same Goal: Reliable Controllers

(with minimal resource consumption)

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The main components of a controller  
a set of tasks:  $P_1, P_2 \dots P_n$  running on  
a platform (RTOS: scheduler)

$P_1 \parallel P_2 \parallel \dots \parallel P_n \parallel \text{Scheduler}$

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## The design problem

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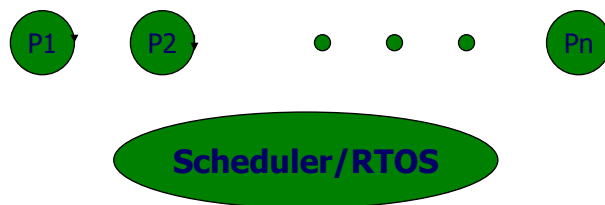
- A set of computation tasks
  - Timing constraints: e.g. Deadlines
  - (QoS constraints: 80% of deadlines met, liveness?)
  - Release patterns i.e Task models
- Design a controller/Schedule
  - To ensure the constraints

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## "Classic" Real Time Scheduling

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- Periodic tasks



- well-developed techniques e.g. Rate-Monotonic Scheduling

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## Rate-Monotonic Scheduling

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- $P_1 \dots P_n$  arrive at **fixed rates**
- Fixed Priority Order: **Higher frequency  $\Rightarrow$  Higher priority**
- Always run the task with highest priority (FPS)  
 $P_1 \parallel P_2 \parallel \dots \parallel P_n \parallel \text{FPS}$
- Schedulability can be tested by utilization bound (or equation solving)

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## In real life, **tasks** may

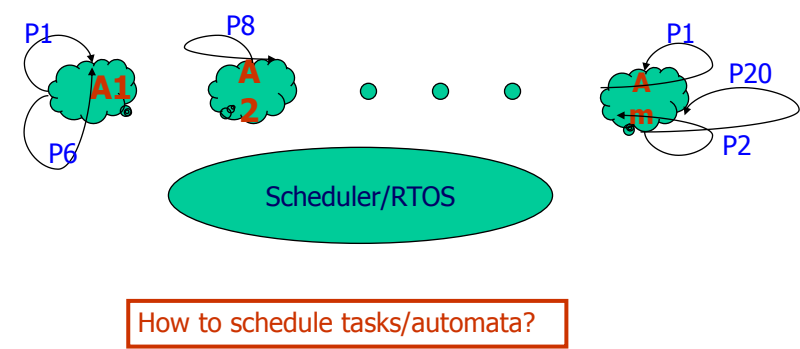
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- share many resources (not only CPU time)
- have complex control structures and interactions
- have to satisfy mixed logical, temporal & resource constraints

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# Automata-based Approaches

A controller = a set of **timed automata** accepting tasks  $P_i$ 's



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## The TIMES project

Tools for Modeling and Implementation of Embedded Systems

Uppsala University

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# Vision

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- Timed Model to Executable Code  
Guaranteeing Timing Constraints
- Timing analysis of Concurrent and Time-Critical Software
  - Response time estimation

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## Problems to solve

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- Schedulability analysis: check  
(A1 || A2 || ... || An || Scheduler) satisfies K
  - A scheduler is given e.g. FPS, RMS, EDF etc
  - K is a requirement specifying e.g. safety & liveness
- Schedule synthesis: find X such that  
(A1 || A2 || ... || An || X) satisfies K

**All these can be automated**

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## OUTLINE

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- A Model for Timed Systems [1998]
    - Timed automata with tasks
  - Schedulability and (un)Decidability [TACAS 02, IC 07]
    - Timed automata with bounded subtraction
  - More Efficient Algorithms [TACAS 03, TCS 06]
    - Schedulability analysis using 2 clocks
    - (similar to Rate-Monotonic Scheduling)
  - TIMES demo
- Implemented in the TIMES tool**

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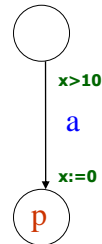
# The MODEL

(Timed Automata with Tasks)

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# Modelling Real Time Systems

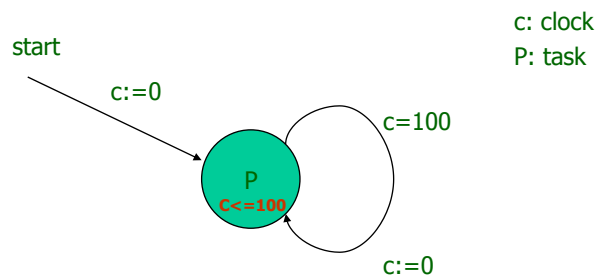
- Events
  - synchronization
  - interrupts
- Timing constraints
  - specifying event arrivals
  - e.g. Periodic and sporadic
- Tasks (executable programs)
  - interrupt processing
  - Internal computation
  - triggered by events and scheduled in the ready queue of RTOS



**Timed Automaton**  
**+ tasks**

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## Example: periodic tasks



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## Tasks = Executable Programs (e.g. C, Java)

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- Task parameters:
  - C: WCET
  - D: Relative Deadline
  - (other parameters for scheduling e.g. Priority)

- Task Interface:

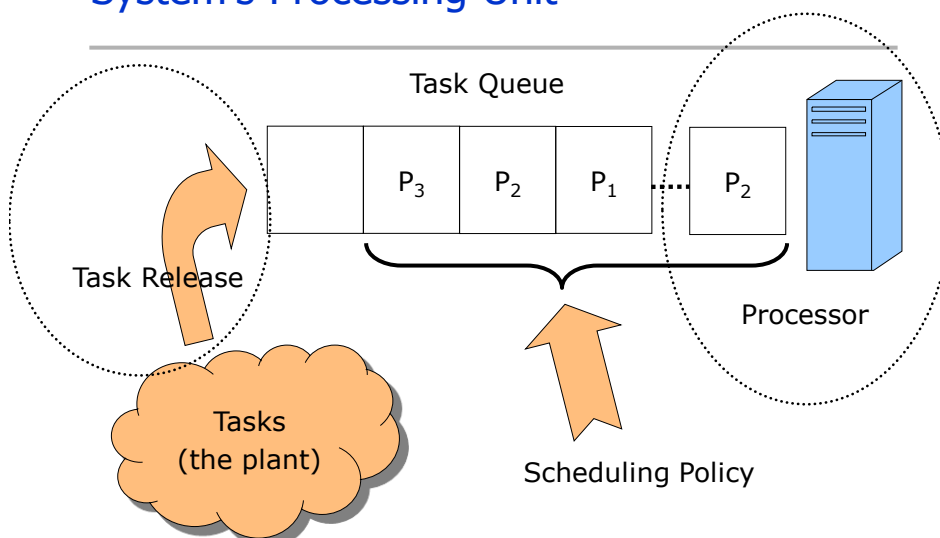
```
Task P  
{  
   $v_1 := F_1(v_1 \dots v_n)$   
  ...  
   $v_n := F_n(v_1 \dots v_n)$   
}
```

(a set of variables updated)

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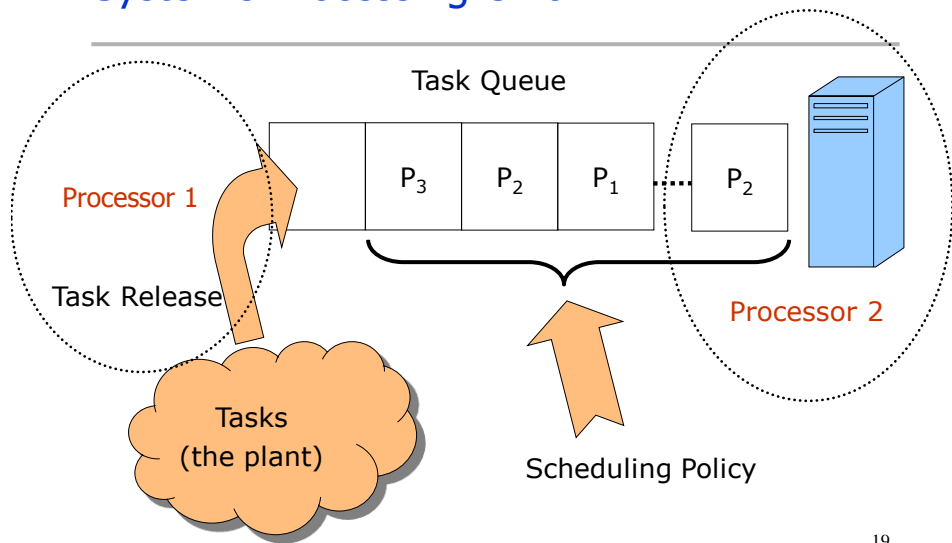
## System's Processing Unit

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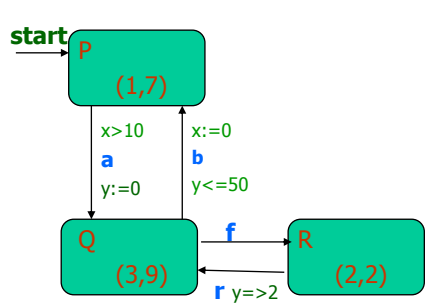
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# System's Processing Unit



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## Timed Automata with Tasks (Example)



- Processor 1 (event handler)**
  - Initially, **P** in the queue
  - Run-to-Completion/Stablization
    - Whenever **a** available and  $x > 10$ , **Q** is put in the queue
    - Then
      - Whenever **b** available and  $y \leq 50$ , **P** is put in the queue
      - Whenever **f** available, **R** is put in the queue.
- Processor 2 (task handler)**
  - Schedule and Compute tasks in the queue



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## Timed Automata with Tasks [1998]

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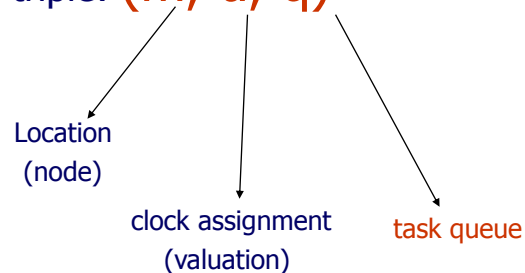
- Assume a set of tasks  $\Pr$
- A timed automaton with tasks is a tuple:  $\langle N, n_0, T, M \rangle$ 
  - $\langle N, n_0, T \rangle$  is a standard timed automaton
    - $N$  is a set of nodes
    - $n_0$  is the initial node
    - $T \subseteq N \times (B(C) \times \text{Act} \times 2^C) \times N$  is the set of 'edges'
      - $C$  is a set of clocks
      - $\text{Act}$  is a set of actions
      - $B(C)$  is the set of clock constraints e.g.  $X < 10$  etc
  - $M: N \rightarrow 2^{\Pr}$  is a mapping which assigns each node a set of tasks

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## States/Configurations of automata

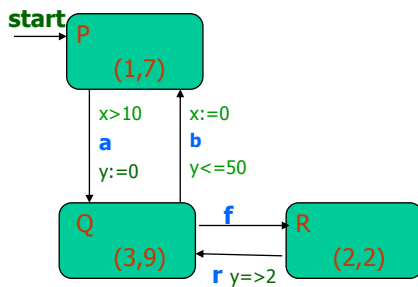
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A state is a triple:  $(m, u, q)$



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## Example



Initial State:  $(P, x=y=0, [P(1,7)])$

Example transitions:

$(P, x=y=0, [P(1,7)]) \xrightarrow{-0.6} (P, x=y=0.6, [P(0.4, 6.4)]) \xrightarrow{-9.5} (P, x=y=10.1, []) \xrightarrow{-a} (Q, x=10.1, y=0, [Q(3,9)]) \xrightarrow{-f} (R, x=10.1, y=0, [Q(3,9), R(2,2)]) \xrightarrow{-2} (R, x=12.1, y=2, [Q(3,7)]) \xrightarrow{-r} (Q, x=12.1, y=2, [Q(3,7), Q(3,9)]) \xrightarrow{-b} (P, x=0, y=2, [Q(3,7), Q(3,9), P(1,7)]) \dots$

We need to handle the queue by **Run** and **Sch**

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## Sch and Run

- Sch** is a function sorting task queues according to a given scheduling strategy e.g FPS, EDF, FIFO etc

Example:  $\text{EDF} [P(2, 10), Q(4, 7)] = [Q(4, 7), P(2, 10)]$

- Run** is a function corresponding to running the first task of the queue for a given amount of time.

Examples:  $\text{Run}(0.5, [Q(4, 7), P(2, 10)]) = [Q(3.5, 6.5), P(2, 9.5)]$

$\text{Run}(5, [Q(4, 7), P(2, 10)]) = [P(1, 5)]$

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## Semantics (as transition systems)

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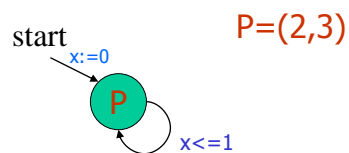
- **States:**  $\langle m, u, q \rangle$ 
  - $m$  is a location
  - $u$  is a clock assignment (valuation)
  - $q$  is a queue of tasks (ready to run)
- **Transitions:**
  1.  $\langle m, u, q \rangle \xrightarrow{a} \langle n, r(u), \text{Sch}[M(n)::q] \rangle$  if  $\textcircled{m} \xrightarrow{g \ a \ r} \textcircled{n}$  &  $g(u)$
  2.  $\langle m, u, q \rangle \xrightarrow{d} \langle m, u+d, \text{Run}(d, q) \rangle$  where  $d$  is a real

**OBS:**  $q$  is growing (by actions) and shrinking (by delays)

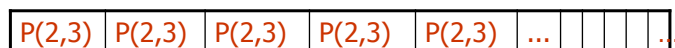
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## Zenoness = Non-Schedulability

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**Zeno:**  $\infty$  many  $P$ 's may arrive within 1 time unit !



But after 2 copies, the queue will be **non-schedulable**

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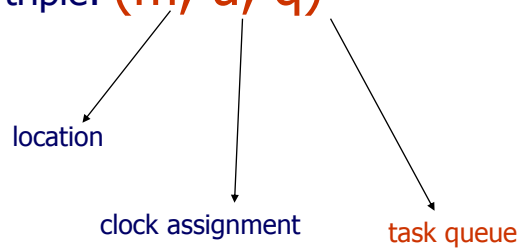
# SCHEDULABILITY

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## Schedulability of automata

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a state is a triple:  $(m, u, q)$



- A state is schedulable if  $q$  is schedulable
- An automaton is schedulable if all reachable states are

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## Schedulability of Automata

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Assume a scheduling policy  $Sch$ :

- A state  $(m, u, q)$  is schedulable with  $Sch$  if
  - $Sch(q) = [P_1(c_1, d_1)P_2(c_2, d_2) \dots P_n(c_n, d_n)]$  and
  - $(c_1 + \dots + c_i) \leq d_i$  for all  $i \leq n$  (i.e. all deadlines met)
- An automaton is schedulable with  $Sch$  if all its reachable states are schedulable
- An automaton is schedulable with a class of scheduling policies if it is schedulable with every  $Sch$  in the class.

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## Other verification/scheduling problems

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- Location Reachability (just as for timed automata)
  - a nice property of the model !
- Boundedness of the task queue  $|q| < M$ 
  - memory requirement
- Schedule synthesis

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# DECIDABILITY

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## Schedulability Analysis (Non-preemptive scheduling)

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FACT [1998]

For Non-preemptive scheduling strategies,  
the schedulability of an automaton can be checked  
by reachability analysis on ordinary timed automata.

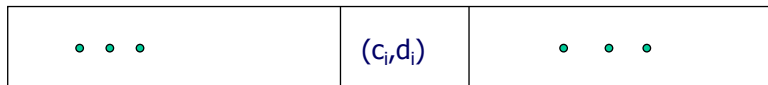
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## Proof ideas (1):

Size of schedulable queues is bounded

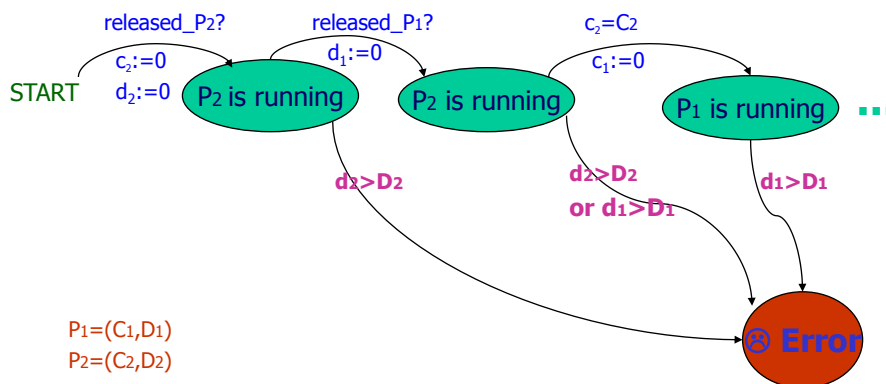
- The maximal number of instances of  $P_i$  in a schedulable queue is bounded by  $M_i = \lceil D_i/C_i \rceil$
- The maximal size of schedulable queues is bounded by  $M_1 + M_2 + \dots + M_n$
- To code the queue/scheduler, for each task instance, use 2 clocks:
  - $c_i$  remembers the computing time
  - $d_i$  remembers the deadline



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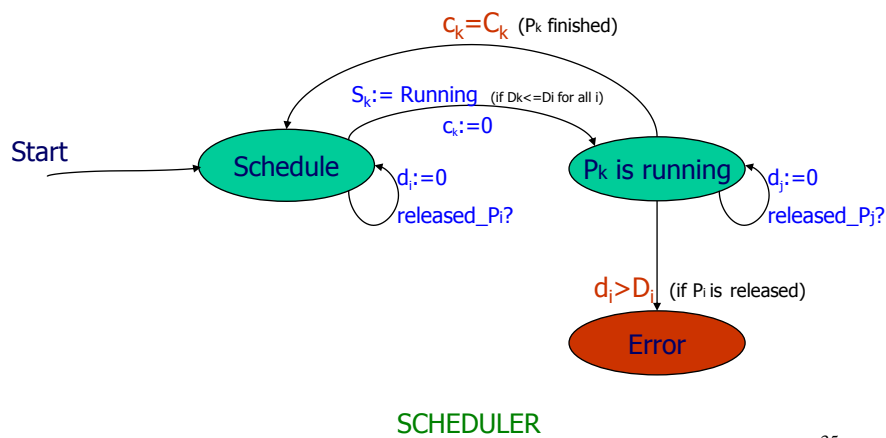
## Proof ideas (2):

The scheduler as an automaton



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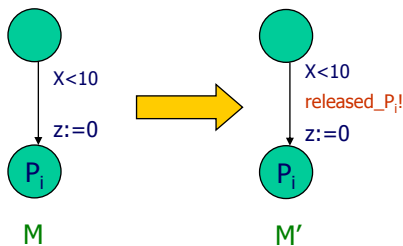
# The scheduler automaton



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## Proof Ideas (3)

- Modify the original automaton **M**: adding 'release!' to inform the scheduler



- Check reachability of the **error** state for  $M' \parallel \text{SCHEDULER}$

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## How about preemptive scheduling?

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- We may try the same ideas
  - Use clocks to remember computing times and deadlines
- BUT a running task may be stopped to run a more 'urgent' task
  - Thus we need stop-watches to remember computing times

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## Conjecture (1998):

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- The schedulability problem for Preemptive scheduling is undecidable.
- The intuition: we need stop-watch to code the scheduler and the reachability problem for stop-watch automata is undecidable
- This is wrong !!!

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## Decidability Result [TACAS 2002]

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### FACT

For Preemptive scheduling strategies, the schedulability of an automaton can be checked by reachability analysis on Bounded Subtraction Timed Automata (BSA).

### NOTE

- Reachability for BSA is decidable
- Preemptive EDF is optimal; thus the general schedulability checking problem is decidable.

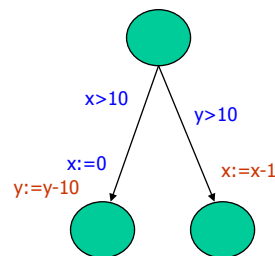
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## Timed automata with subtraction

i.e. Subtraction Automata, [McManis and Varaiya, CAV94]

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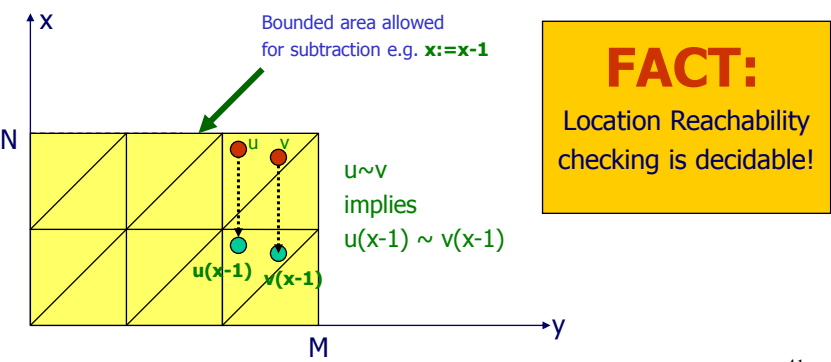
- Subtraction automata are timed automata extended with subtraction on clocks
- That is, in addition to reset  $x:=0$ , it is also allowed to update a clock  $x$  with  $x:=x-n$  where  $n$  is a natural number



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# Bounded Subtraction Automata

- A subtraction automaton is bounded if its clocks are non-negative and bounded with a maximal constant (or subtraction is only allowed in the bounded zone).

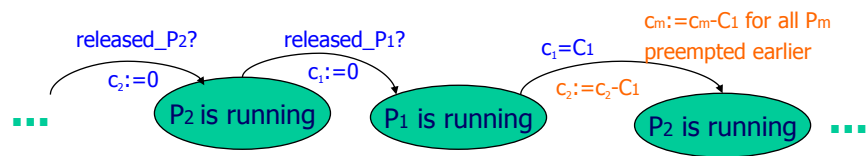


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## Schedulability Checking as a reachability problem for Bounded Subtraction Automata

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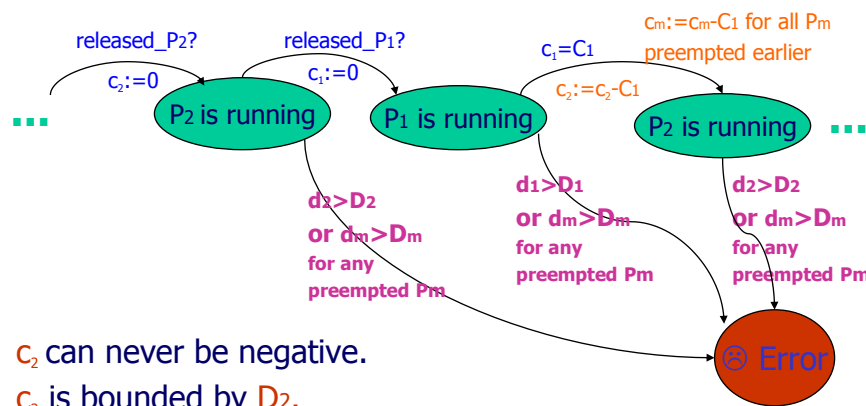
# Proof ideas (no stop but subtraction :-)



- Model the scheduler as a subtraction automaton
  - Do not stop the computing clock  $c_2$  when a new task  $P_1$  is released
  - Let  $c_2$  for  $P_2$  (preempted) run until the task  $P_1$  (with higher priority) finishes, then perform  $c_2 := c_2 - C_1$  (note:  $C_1$  is the computing time for  $P_1$ ).

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# Proof ideas (clocks are bounded):



- $c_2$  can never be negative.
- $c_2$  is bounded by  $D_2$ .

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# END of proof

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## Complexity

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#clocks (needed)

= 2 x #instances (maximal number of schedulable task instances)

= 2 x  $\sum_i \lceil D_i / C_i \rceil$

This is a huge number in the worst case  
But the run-time complexity is not so bad!

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## It works anyway !!!

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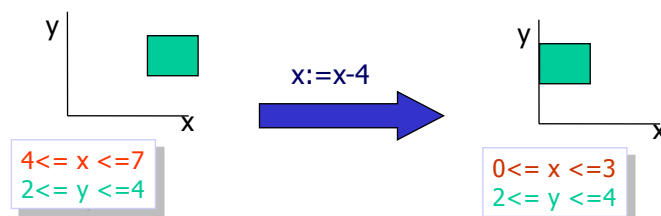
- #active tasks in the queue is normally small, and the run-time complexity is only related to #active clocks
- If Too many active tasks in the queue (i.e. Too many active clocks), the check will stop sooner and report "non-schedulable"
- AND the analysis can be done symbolically!

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## Schedulability analysis based on Constraints (DBM's)

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Subtraction on Clocks, added to DBM-library (UPPAAL, Kronos)



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**WE CAN DO BETTER !** [TACAS 03]

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For **fixed priority** scheduling strategies (FPS),  
we need only **2 clocks** (and ordinary timed automata)!

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## The 2-CLOCK ENCODING

(for **fixed-priority** scheduling strategies)

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## Main Idea

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- Check the schedulability of tasks **one by one** according to priority order (highest priority first)
- This is similar to response time analysis in **RMS**

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To code the queue/scheduler, we need:

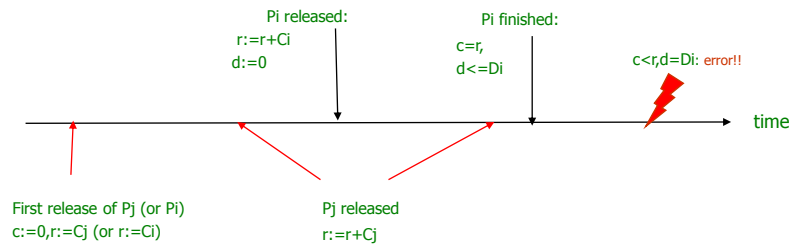
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- 1 integer variable for **Pi**:
  - **r** denotes the response time as in RMS  
(the total computing time needed before Pi finishes)
- 2 clocks for **Pi**:
  - **c** remembers the accumulated computing time  
(so much has been computed so far)
  - **d** remembers the "deadline"

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## Intuition of the encoding: $R_i = C_i + \sum_{\text{pri}(P_j) > \text{pri}(P_i)} C_j$

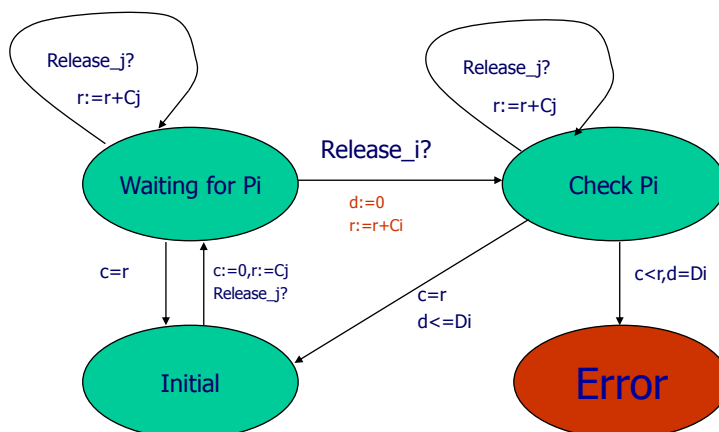
- Assume:  $\text{priority}(P_j) > \text{priority}(P_i)$  and  $P_i$  is analyzed



When  $P_i$  finishes,  $r = R_i$

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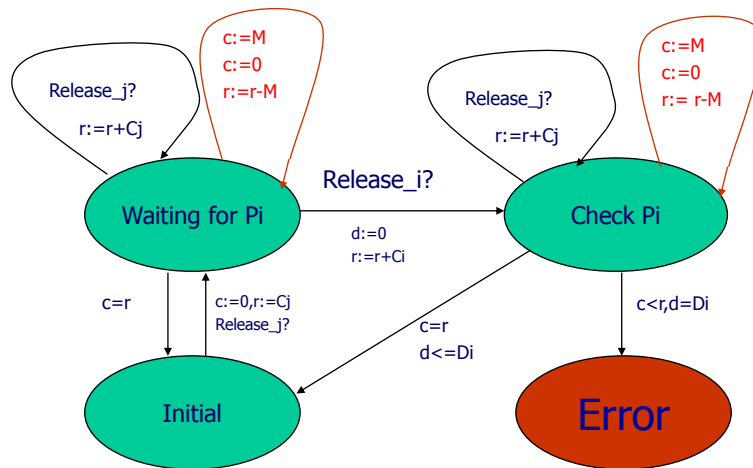
## The "FPS scheduler": analyzing $P_i$



Note that it is not clear that  $c$  and  $r$  are not bounded !

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## The "FPS scheduler": analyzing $P_i$ (we need the boundedness)



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OBS:  $r-c$  is the only interesting info, so  $M$  can be any integer! Let  $M=C_i$

## $c$ and $r$ are bounded

- $c$  is bounded by  $M$
- $r$  is bounded by  $r_{\max} + C_i$ 
  - Where  $r_{\max}$  is the maximal value of  $r$  from previous analysis for all tasks  $P_j$  with higher priority

So the scheduler is a standard TA **END**

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## Decidability results

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- For Non-preemptive scheduling, the problem can be solved using TA.
- For preemptive scheduling, the problem can be solved using BSA (Bounded Subtraction Automata) [TACAS02]
- For **fixed-priority scheduling**, the problem can be solved using TA with only **2 extra clocks** – similar to the classic RMA technique (Rate-Monotonic Analysis) [TACAS03]

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## Undecidability [TACAS 04]

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Unfortunately, the problem will be undecidable if the following Conditions hold together:

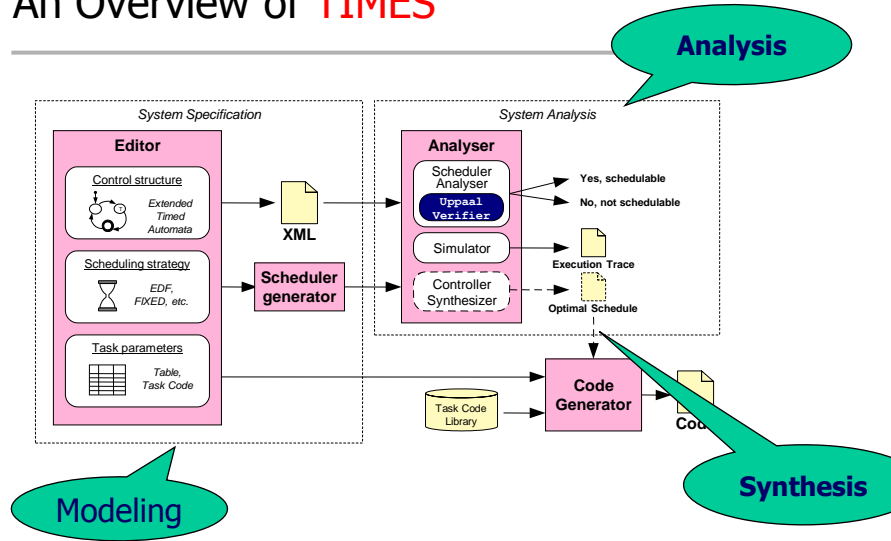
1. Preemptive scheduling
2. Interval computation times
3. Feedback i.e. **the finishing time of tasks may influence the release times of new tasks.**

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An Overview of TIMES

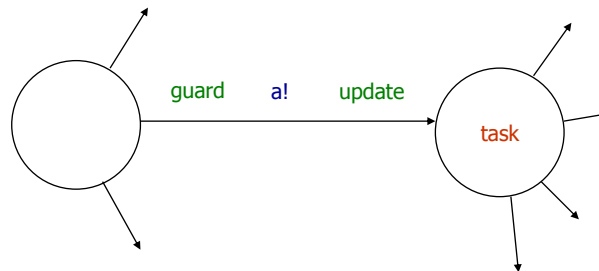


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## The **INPUT LANGUAGE** is very much like **"guarded commands"**

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OBS: **guard** and **update** may contain data variables (integer, array)



- **guard, update**: "synchronous" computation which takes "no time"
  - we adopt the **synchronous hypothesis**
- **task**: "asynchronous" computation which takes time

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## Tasks = Executable Programs (e.g. C, Java)

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- Task Type
  - **Synchronous or Asynchronous**
  - **Non-Periodic** (triggered by events) or **Periodic**
- Task parameters: **C, D** etc
  - **C**: Computing time and **D**: Relative Deadline
  - other parameters for scheduling e.g. **priority, period**
- Task Interface (variables updated '**atomically**')
  - $X_i := F_i(X_1 \dots X_n)$
- Tasks may have shared variables
  - with **automata**
  - with **other tasks** (**priority ceiling protocols**)
- Tasks with Precedence constraints

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## Functionality/Features of TIMES

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- GUI
  - Modeling: automata with (a)synchronous tasks
  - editing, task library, visualization etc
- Simulation
  - Symbolic execution as MSC's and Gant Charts
- Verification
  - Safety, bounded liveness properties (all you do with UPPAAL)
  - Schedulability analysis
- Synthesis
  - Verified executable code (guaranteeing timing constraints)
    - $\text{Traces}(\text{Code}) \subseteq \text{Traces}(\text{Model})$
  - Schedule synthesis (ongoing)

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## CODE SYNTHESIS in TIMES

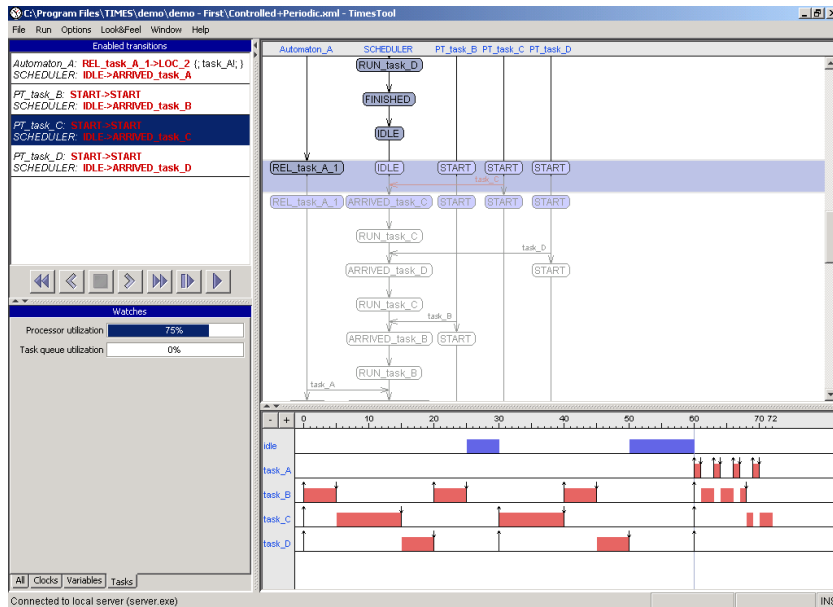
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- Run Time Systems
  - Event Handler
    - OS interrupt processing system or Polling
  - Task scheduler
    - generated from task parameters
- Application Tasks = threads (or processes)
  - Already there! (written in C)
  - Current version of TIMES support LegoOS !

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# TIMES demo



## Conclusions/Remarks

- A unified model for timed systems (can express synchronization, computation and complex temporal and resource constraints).
- The first decidability result (and efficient algorithms) for preemptive scheduling in dense time models:
  - The analysis is symbolic (using DBM's in the UPPAAL tool)
  - The results can be adopted for schedulability analysis of message transmission.
- Implementation: **TIMES**