

Your exam code:

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# Final Exam (Part 2) in Program Design and Data Structures (1DL201)

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Bergsbrunnagatan 15, room 1  
2015-03-19 / 8:00–13:00

## Instructions

Read and follow these instructions carefully to increase your chance of getting good marks.

- This is a closed book exam. You may use a standard English dictionary. Otherwise, **no notes, calculators, mobile phones, or other electronic devices are allowed**. Cheating will not be tolerated.
- Read and follow the instructions on the front sheet.
- In the table below, clearly mark **at most one** answer for each question. (If you think that a question is ambiguous or has no correct answer, mark the question number with a ★ and explain on a separate sheet of paper what the problem is and what assumptions you have made to answer the question.)
- Dave Clarke will come to the exam hall around 9:30 to answer questions.

Good luck!

## Your Answers

Question	Answer					Question	Answer				
1	A	B	C	D	E	11	A	B	C	D	E
2	A	B	C	D	E	12	A	B	C	D	E
3	A	B	C	D	E	13	A	B	C	D	E
4	A	B	C	D	E	14	A	B	C	D	E
5	A	B	C	D	E	15	A	B	C	D	E
6	A	B	C	D	E	16	A	B	C	D	E
7	A	B	C	D	E	17	A	B	C	D	E
8	A	B	C	D	E	18	A	B	C	D	E
9	A	B	C	D	E	19	A	B	C	D	E
10	A	B	C	D	E	20	A	B	C	D	E



# Questions

Please choose a single answer for each question. Read the questions carefully, and watch out for negations (*not*, *except*, etc.).

1. Consider the following function.

```
lookup :: Eq a => a -> AssocList a b -> Maybe b
lookup _ [] = Nothing
lookup k ((x,y):xs) = if x==k then Just y else lookup k xs
```

Which of the following type declarations will make the above code type-correct?

- (A) `type AssocList a b = a -> Maybe b`
- (B) `type AssocList = (x,y):xs`
- (C) `type AssocList a b = [(a,Maybe b)]`
- (D) `type AssocList a b = [(a,b)]`
- (E) `type AssocList a b = Eq a => Maybe b`

Answer: (D)

2. Suppose you want to define a datatype to model *snarps*. You have no idea what a snarp is, but you have been told that there are only three kinds of them:

- (i) the *grob* is a special snarp (that is different from all other snarps),
- (ii) every string is a different snarp, and
- (iii) one can *gister* any snarp and any integer to obtain a new snarp.

Which datatype definition would you use?

- (A) `data Snarp = Snarp Grob String (Snarp,Integer)`
- (B) `data Snarp = Grob | Str String | Gister Snarp Integer`
- (C) `data Snarp = Grob | String | Gister`
- (D) `data Snarp = Snarp Grob | Snarp String | Snarp Snarp Integer`
- (E) `data Snarp = Grob Snarp | Str String | Gister Snarp Integer`

Answer: (B)

3. Consider the type of general trees, defined as

```
data Tree a = Node a [Tree a]
```

What does the following function `f` compute?

```
f (Node a ts) = a : fs ts

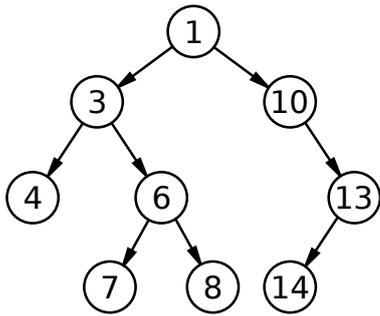
fs [] = []
fs (t:ts) = f t ++ fs ts
```

- (A) The number of nodes in a tree.
- (B) A post-order list of all values in a tree.
- (C) The height of a tree.
- (D) A pre-order list of all values in a tree.
- (E) The sum of all values in a tree.

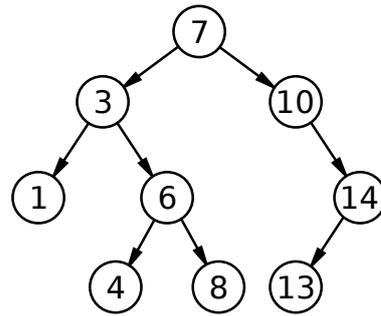
Answer: (D)

4. Which of the following trees is a binary search tree?

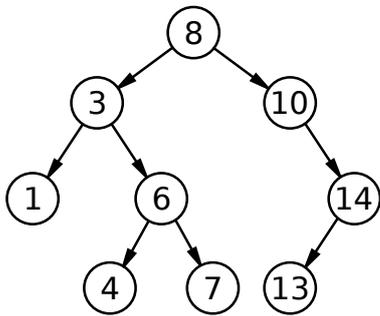
(A)



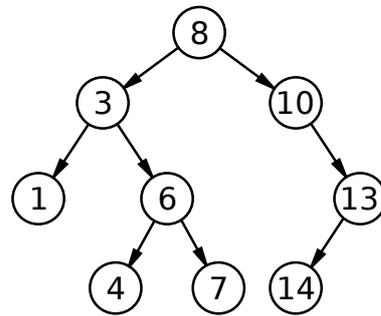
(B)



(C)



(D)



(E) None of these.

Answer: (C)

5. The (worst-case) complexity of searching in a binary search tree with  $n$  nodes is

- (A)  $O(n^2)$       (B)  $O(2^n)$       (C)  $O(n)$       (D)  $O(1)$       (E)  $O(\log n)$

Answer: (C)

6. Which of the following statements about Abstract Datatypes (ADTs) is **false**?

- (A) ADTs make it easier to preserve representation invariants.
- (B) Pattern matching is not available on ADTs.
- (C) The client of an ADT is independent of the ADT's specific representation.
- (D) ADTs support programming to an interface.
- (E) ADTs are more efficient than regular datatypes.

Answer: (E) ADTs often introduce overhead.

7. Assume that the the module `Table` includes the following declaration:

```
module Table(Table, empty, insert, exists, lookup, delete,
             iterate, keys, values) where
```

Client code imports `Table` using the following import statement:

```
import qualified Table(empty,insert) as T hiding(exists)
```

Which additional names does this import statement introduce into the code?

- (A) `empty`, `insert`
- (B) `T.empty`, `T.insert`
- (C) `Table`, `empty`, `insert`, `exists`, `lookup`, `delete`, `iterate`, `keys`, `values`
- (D) `Table`, `empty`, `insert`, `lookup`, `delete`, `iterate`, `keys`, `values`
- (E) `empty`, `insert`, `T.empty`, `T.insert`

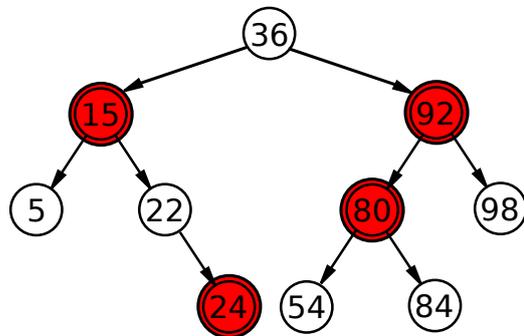
Answer: (B)

8. Suppose the following numbers are inserted, in the given order, into an initially empty red-black tree. (Grey=red.)

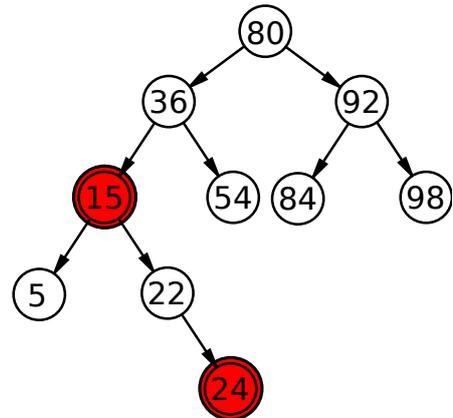
22 36 84 92 24 5 15 80 98 54

What is the resulting red-black tree?

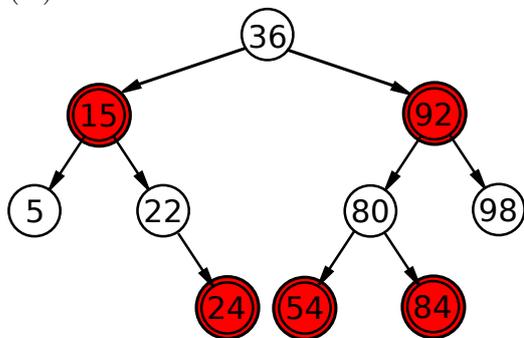
(A)



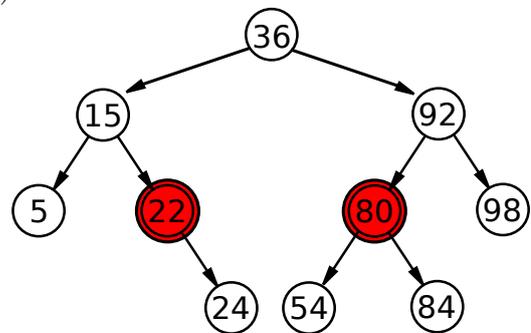
(B)



(C)



(D)



(E) None of these.

Answer: (B)

9. The (worst-case) complexity of inserting an item into a red-black tree with  $n$  nodes is
- (A)  $O(1)$       (B)  $O(n)$       (C)  $O(2^n)$       (D)  $O(\log n)$       (E)  $O(n^2)$

Answer: (D)

10. The function `unsafePerformIO :: IO a -> a` from module `System.IO.Unsafe` is considered unsafe. It can be used to embed imperative code into pure code.

Why is `unsafePerformIO` considered to be unsafe?

- (A) Using it properly requires advanced programming skills.  
(B) It invalidates Haskell's optimisations.  
(C) It violates purity.  
(D) It can result in I/O operations occurring in unexpected orders.  
(E) All of the above.

Answer: (E) It's really bad.

11. Given the following datatype

```
data Tree a b = Leaf a | Branch b (Tree a b) (Tree a b)
```

and the following typeclass

```
class Foo a where
  foo :: a -> Int
```

with the following instances

```
instance Foo Bool where
  foo True = 1
  foo False = 0
```

```
instance Foo Int where
  foo n = n `mod` 5
```

```
instance (Foo a, Foo b) => Foo (Tree a b) where
  foo (Leaf a) = foo a
  foo (Branch a b c) = (foo a + foo b + foo c) `mod` 5
```

```
instance Foo a => Foo [a] where
  foo l = (sum (map foo l)) `mod` 5
```

What is the value of

```
foo $ Branch True (Leaf [1::Int,2,3])
      (Branch False (Leaf [0,3]) (Leaf [2,5]))
```

- (A) 0      (B) 1      (C) 2      (D) 3      (E) 4

Answer: (C)

12. Consider the following function:

```
saywhat a b = if a < foo b then show a else show b
```

What type will Haskell give to this function, where `foo` is the function belonging to the type class in the previous question?

- (A) `Int -> Int -> String`
- (B) `(Foo a, Ord a) => Int -> a -> String`
- (C) `(Show a) => Int -> a -> String`
- (D) `(Foo a, Show a) => Int -> a -> String`
- (E) `(Foo a, Ord a, Show a) => Int -> a -> String`

Answer: (D)

13. The purpose of monads in Haskell is:

- (A) to make functional code look like imperative code.
- (B) to enable I/O.
- (C) to introduce the `do`-notation.
- (D) to enable the mixing of pure and impure computation.
- (E) to take something beautiful and make it ugly.

Answer: (D)

14. Consider the following interface to a stack datatype:

```
empty :: Stack a
isEmpty :: Stack a -> Bool
push :: a -> Stack a -> Stack a
top :: Stack a -> a
pop :: Stack a -> Stack a
```

with the same semantics as considered in class. What is the value of

```
top $ pop $ push 15 $ push 12 $ push 10 empty
```

- (A) A stack containing 15 and 12
- (B) A stack containing 12 and 10
- (C) 10
- (D) 15
- (E) 12

Answer: (E)

15. The following code is broken:

```
0. broken = do
1.   putStrLn $ "Enter "
2.     ++ "your " ++ "name: "
3.   let x = getLine
4.       y <- putStrLn "Thank you"
5.       x
```

Running the code in GHCi results in the following:

```
*Main> broken
Enter your name:
Thank you
Dave
"Dave"
```

The first `Dave` is the input entered by the user and the second "Dave" is the result of the function.

Why does `Thank you` appear before the user inputs his name!?!

Which line is the **cause** of the bug?

- (A) 1                      (B) 2                      (C) 3                      (D) 4                      (E) 5

**Answer: (C)**

16. Consider the following hash table of 11 cells, where  $\perp$  denotes that a cell was never used and  $\Delta$  denotes that the element in a cell has been deleted.

0	1	2	3	4	5	6	7	8	9	10
33	23	57	$\Delta$	70	$\perp$	6	$\perp$	19	$\perp$	54

Assume that the hash function is  $h(k) = k \bmod 11$ , that open addressing with linear probing function  $f(i) = i$  is used as the conflict resolution method, and that duplicates are allowed.

In which cell will key 109 be placed?

- (A) 9                      (B) 5                      (C) 3                      (D) 10                      (E) Nowhere.

**Answer: (C)**

17. Recall that the function `random` has type `random :: (Random a, RandomGen g) => g -> (a, g)`. You write the following code to generate three random coin tosses (where `head = True` and `tails = False`).

```
import System.Random

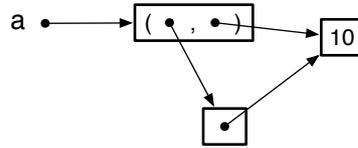
threeCoins :: (Bool, Bool, Bool)
threeCoins =
  let gen = (mkStdGen 21)
  in (fst (random gen), fst (random gen), fst (random gen))
```

Which of the following sentences **best** describes `threeCoins`?

- (A) Oh dear!  
(B) `threeCoins` gives the same value each time it is accessed, and the three coins are equal to each other.  
(C) `threeCoins` gives the same value each time it is accessed, but the three coins may be different from each other.  
(D) `threeCoins` generates different values each time it is accessed, but the three coins are always equal to each other.  
(E) `threeCoins` generates different values each time it is accessed, and the three coins may be different from each other.

**Answer: (B)**

18. The following depicts the under-the-hood structure of a mystery Haskell expression stored in variable `a`. The arrows represent references.

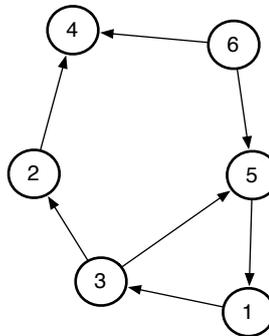


Which of the following is a possible type of `a`?

- (A) `(Int, Int)`      (B) `(IORef Int, Int)`      (C) `IORef (IORef Int, Int)`  
 (D) `IORef (IORef (IORef Int), IORef Int)`      (E) `IORef (IORef Int, IORef Int)`

Answer: (D)

19. Consider the following directed graph:



Which of the following is a valid depth-first search ordering—that is, the order in which nodes are visited when performing a depth-first search?

- (A) 123456      (B) 324516      (C) 135264      (D) 654321      (E) 651342

Answer: (B)

20. Which of the following corresponds to the adjacency list representation of the graph from the previous question?

(A)

	1	2	3	4	5	6
1			1		1	
2			1	1		
3	1	1			1	
4		1				1
5	1		1			1
6				1	1	

(B)

	1	2	3	4	5	6
1			1			
2				1		
3		1			1	
4						
5	1					
6				1	1	

(C)

1	3
2	4
3	2, 5
4	
5	1
6	4, 5

(D)

1	3, 5
2	3, 4
3	1, 2, 5
4	2, 6
5	3, 1
6	4, 6

(E) (1,3), (3,2), (3,5), (2,4), (6,5), (6,4), (5,1)

Answer: (C)