

CORRECTED

Final Exam (Part 1) in Program Design and Data Structures (1DL201)

Teachers: Johannes Borgström, Dave Clarke

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Instructions

Read and follow these instructions carefully to increase your chance of getting good marks.

- This is a closed book exam. You may use a standard English dictionary. Otherwise, **no notes, calculators, mobile phones, or other electronic devices are allowed.** Cheating will not be tolerated.
- This is a multiple-choice exam. Each question has exactly **one** correct answer.
- You may keep these question sheets. **Only hand in the answer sheet.** Also read the instructions on the answer sheet before you start.
- Johannes or Dave will come to the exam hall around 10:00 to answer questions.

Good luck!

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Question 5: Which of the following is a variant (?VARIANT?) for the function `func1 r a ls`?

- A `length ls + length r` `2 * length ls`
 B `length ls - 1`
 C `length r` E `length ls - length r`

Question 6: Which of the following modifications to the definition of `func` (or `func1`) will reverse the order of the list returned from `func`?

- A replace `func1 []` by `reverse.(func1 [])`.
 B replace `func1 r - [] = r` by `func1 r - [] = reverse r`.
 C replace `((x,y):ls)` by `(ls++[(x,y)])`.
 D replace `y:r` by `r ++ y`.
 E replace `x==a` by `a==y`.

Question 7: Which of the following expressions **does not** evaluate to 15?

- `36 'mod' 3 * 7` C `7 - 3 + 11` E `11 'div' 3 * 5`
 B `9 / 3 * 5` D `[3,5] !! 1 * 3`

Question 8: Consider the expression

```
let f x y = x + 3 >= y + 3.1 in f 1 1
```

Evaluating this expression will result in ...

- A True C a type error. none of these.
 B a syntax error. D a run-time error.

Question 9: Consider the declaration

```
f x = let f x = x+1 in f (f x)
```

Which of the following is equivalent to the declaration above?

- A `f z = let g y = z+1 in g (g z)`
 B `f x = let f y = y+1 in f (f y)`
 `f x = let g z = z+1 in g (g x)`
 D `f y = let g y = y+1 in f (f y)`
 E None of these.

Question 10: Consider the function

```
zip (x:xs) (y:ys) = (x,y) : zip xs ys
zip _ _ = []
```

Which of the following expressions is **not** a variant for `zip xs ys`?

- A `length ys` D `length xs + length ys`
 B `length xs`
 C `length xs * length ys` `abs (length xs - length ys)`

Question 11: Which of the following evaluates to 11?

- A `foldr (*) 0 [1,7,3]` D `foldr (+) 1 [1,5,3]`
 B `foldr (+) 0 [1,7,3]`
 C `foldr (*) 1 [1,7,3]` E `foldr (:) [] [1,5,3]`

Question 12: What is the type of `bar`, which is defined as follows:

```
bar f g a = f (g a) a
```

- A $(a \rightarrow b \rightarrow c) \rightarrow (a \rightarrow b) \rightarrow a \rightarrow c$
 B $(a \rightarrow b \rightarrow c) \rightarrow (a \rightarrow b) \rightarrow a \rightarrow c$
 C $((a \rightarrow b \rightarrow c), (b \rightarrow a), b) \rightarrow c$
 D $(a \rightarrow b \rightarrow c) \rightarrow b \rightarrow (a \rightarrow b) \rightarrow c$
 E $(a \rightarrow b \rightarrow c) \rightarrow (b \rightarrow a) \rightarrow a \rightarrow c$

Question 13: Which of the following functions is different from the others — that is, which function gives different results when applied to the same arguments?

- ```
f [] = []
f (x:xs) | x > 2 = x + 10 : f xs
```
- A                      | otherwise = f xs  
 B `f = map (+10) . filter (>2)`  
 C `f xs = [ x + 10 | x <- xs, x > 2]`  
 D `f = map (\x -> x + 10) . filter (\x -> 2 > x)`  
 E `f = filter (>12) . map (+10)`

**Question 14:** Type  $\tau$  is an *instance* of type  $\rho$  if  $\tau$  can be obtained from  $\rho$  by instantiating  $\rho$ 's type variables with other types (which may also be variables). Two types  $\tau$  and  $\rho$  are *related by instantiation* if  $\tau$  is an instance of  $\rho$  or  $\rho$  is an instance of  $\tau$ .

Which of the following types is **not** related to any of the others by instantiation?

- A  $a \rightarrow a$                        D  $(a, a) \rightarrow (a, b)$   
 B  $(a, b) \rightarrow (a, b)$   
 C  $(\text{Int}, a) \rightarrow (\text{Int}, a)$                        E  $(a \rightarrow a) \rightarrow (a \rightarrow a)$

**Question 15:** Recall that  $\Theta(n^3)$  is the set of functions bounded both above and below by  $n^3$ , modulo a constant factor, etc. Which of the following is equal to  $\Theta(n^3)$ ?

- A  $O(n^3) \setminus O(n^2)$                        D  $(O(n^3) \setminus O(n^2)) \cap (\Omega(n^2) \setminus \Omega(n^3))$   
 B  $O(n^3) \cap \Omega(n^3)$   
 C  $\Omega(n^2) \setminus \Omega(n^3)$                        E All of the above

**Question 16:** Consider the following function

```
foo :: ([a] -> b) -> [a] -> [b]
```

```
foo f [] = [f []]
```

```
foo f l@(_:as) = f l : foo f as
```

Assuming that the run-time cost of some function  $g$  is given by  $T_g(n)$ , where  $n$  is the *size* of its input, which of the following recurrences describes the run-time cost of `foo g`?

$$\boxed{\text{A}} \quad T(n) = \begin{cases} T_g(0) & \text{if } n = 0 \\ \Theta(1) + T(n-1) + \Theta(n) & \text{if } n \geq 1 \end{cases}$$

$$\boxed{\text{B}} \quad T(n) = \begin{cases} T_g(0) & \text{if } n = 0 \\ T_g(n) + T(n-1) + \Theta(n) & \text{if } n > 1 \end{cases}$$

$$\boxed{\text{C}} \quad T(n) = \begin{cases} T_g(0) & \text{if } n = 0 \\ T(n) + T(n-1) + \Theta(1) & \text{if } n \geq 1 \end{cases}$$

$$\boxed{\text{D}} \quad T(n) = \begin{cases} T_g(0) & \text{if } n = 1 \\ T_g(n) + T(n-1) + \Theta(n) & \text{if } n > 1 \end{cases}$$

$$\blacksquare \quad T(n) = \begin{cases} T_g(0) & \text{if } n = 0 \\ T_g(n) + T(n-1) + \Theta(1) & \text{if } n \geq 1 \end{cases}$$

**Question 17:** Which of the following recurrences has the closed form  $T(n) = 5n+7$ ?

$$\blacksquare \quad T(n) = \begin{cases} 7 & \text{if } n = 0 \\ T(n-1) + 5 & \text{if } n \geq 1 \end{cases}$$

$$\boxed{\text{B}} \quad T(n) = \begin{cases} 5 & \text{if } n = 0 \\ 2T(n-1) + 7 & \text{if } n \geq 1 \end{cases}$$

$$\boxed{\text{C}} \quad T(n) = \begin{cases} 5 & \text{if } n = 0 \\ 7T(n) + 1 & \text{if } n \geq 1 \end{cases}$$

$$\boxed{\text{D}} \quad T(n) = \begin{cases} 7 & \text{if } n = 0 \\ 5T(n-1) & \text{if } n \geq 1 \end{cases}$$

$$\boxed{\text{E}} \quad T(n) = \begin{cases} 3 & \text{if } n = 0 \\ 5T(n-1) + 4 & \text{if } n \geq 1 \end{cases}$$

**Question 18:** Consider the following datatype declarations.

```
data BTreeA a = Leaf a
 | Node (BTreeA a) a (BTreeA a)
```

```
data BTreeB a = Leaf a
 | Node (BTreeB a) (BTreeB a)
```

```
data BTreeC a = Leaf
 | Node (BTreeC a) a (BTreeC a)
```

```
data BTreeD a = Leaf a
 | Node a (BTreeD a) (BTreeD a)
```

```
data BTreeE a = Leaf a
 | Node (BTreeE a) (BTreeE a) a
```

Which of them can represent trees containing an arbitrary non-negative number of data items?

A BTreeA

B BTreeB

C BTreeC

D BTreeD

E BTreeE

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**Question 19:** Which of the binary tree datatypes defined above admits insertion of a single new data item in constant time (i.e.,  $O(1)$ )?

With insertion is meant an operation `insert :: a -> BTreeX a -> BTreeX a`, where `insert x t` returns a tree containing `x` and the data items in `t` (similar to `(:) :: a -> [a] -> [a]`).

- BTreeB and BTreeC                       BTreeB only  
 BTreeA, BTreeD, and BTreeE  
 BTreeC only                                       All except BTreeB

**Question 20:**

Which of the datatype declarations above **cannot** be used with the standard binary search tree invariant and search algorithm as seen in class?

- BTreeA       BTreeB       BTreeC       BTreeD       BTreeE

