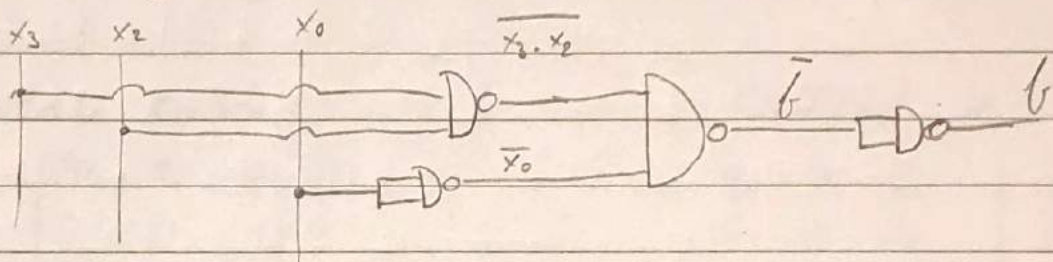


A_1 $x_1 x_0$

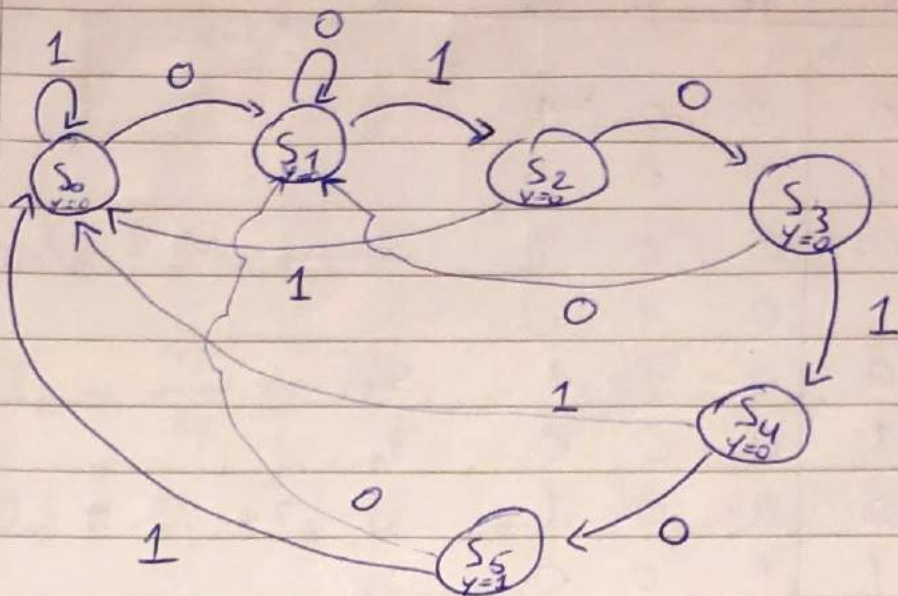
		00	01	11	10
$x_3 x_2$	00	1	-		1
	01	1			-
	11		-		-
	10	1			1

$$f = \overline{x_3} \cdot \overline{x_0} + \overline{x_2} \cdot \overline{x_0} = (\overline{x_3} + \overline{x_2}) \cdot \overline{x_0}$$

$$= \overline{x_3 \cdot x_2} \cdot \overline{x_0}$$



A_2



State coding:

	q_2	q_1	q_0
S_0	0	0	0
S_1	0	0	1
S_2	0	1	0
S_3	0	1	1
S_4	1	0	0
S_5	1	0	1

Output y

q_2	q_1	q_0	y
0	0	0	0
0	0	1	0
0	1	0	0
0	1	1	0
1	0	0	0
1	0	1	1

(missing rows are treated as "don't care")

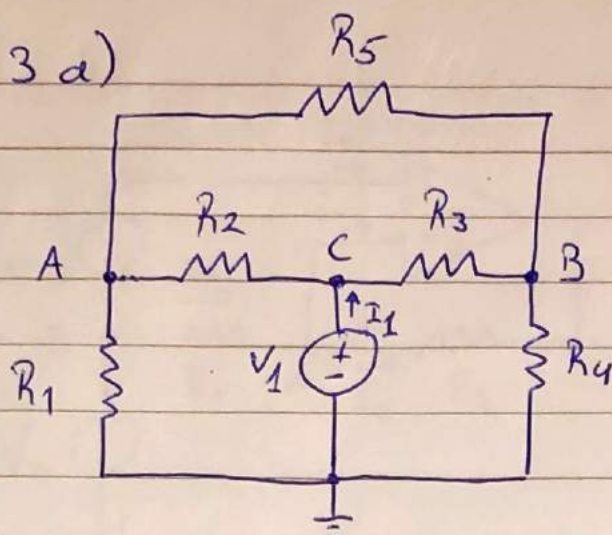
State Transitions

q_2	q_1	q_0	x	q_2^+	q_1^+	q_0^+	
0	0	0	0	0	0	1	S_1
0	0	0	1	0	0	0	S_0
0	0	1	0	0	0	1	S_1
0	0	1	1	0	1	0	S_2
0	1	0	0	0	1	1	S_3
0	1	0	1	0	0	0	S_0
0	1	1	0	0	0	1	S_1
0	1	1	1	1	0	0	S_4
1	0	0	0	1	0	1	S_5
1	0	0	1	0	0	0	S_0
1	0	1	0	0	0	1	S_1
1	0	1	1	0	0	0	S_0

Moore Type, because output y only depends on the states.

3 memory bits are used, so 3 flip-flops are needed.

A3 a)



Using the method of potentials, we label each node as A, B, C, and each voltage with respect to ground is V_A , V_B , V_C .

• $V_C = V_1$, $V_A = ?$, $V_B = ?$

KCL at each node with unknown voltage

$$\begin{aligned} A: & \left\{ \begin{aligned} -\frac{V_A}{R_1} - \frac{V_A - V_C}{R_2} - \frac{V_A - V_B}{R_5} &= 0 \\ B: & \left\{ \begin{aligned} -\frac{V_B}{R_4} - \frac{V_B - V_C}{R_3} - \frac{V_B - V_A}{R_5} &= 0 \end{aligned} \right. \end{aligned} \right. \end{aligned}$$

$$\begin{aligned} (=) & \begin{cases} -\left(\frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_5}\right)V_A + \frac{1}{R_5}V_B = -\frac{V_1}{R_2} \\ \frac{1}{R_5}V_A - \left(\frac{1}{R_3} + \frac{1}{R_4} + \frac{1}{R_5}\right)V_B = -\frac{V_1}{R_3} \end{cases} \end{aligned}$$

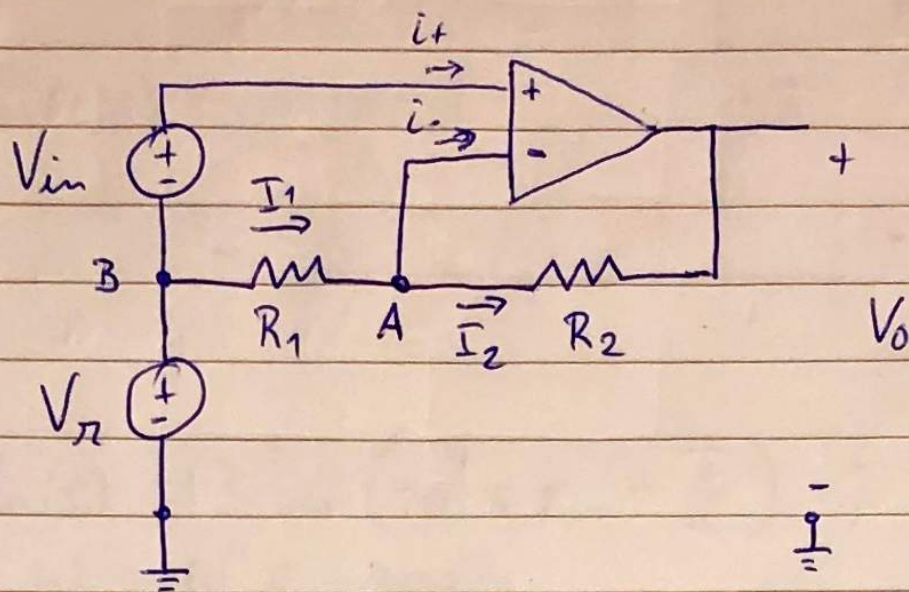
(inserting the values for R 's and V_1 , we get:)

$$V_A = V_B = \frac{R_4}{R_3 + R_4} V_1 = \frac{5}{4} \text{ V}$$

KCL on C:

$$I_1 = \frac{V_1 - V_A}{R_2} + \frac{V_1 - V_B}{R_3} = 250 \text{ mA}$$

A3.b)



OPAMP with negative feedback:

i) $i_+ = i_- = 0$; ii) $V_+ = V_-$

$$V_A = V_- = V_+ = V_{in} + V_{ref} ; V_B = V_{ref}$$

$$\text{KCL at node A: } \underbrace{\frac{V_B - V_A}{R_1}}_{= I_1} - \underbrace{i_-}_{=0} - \underbrace{\frac{V_A - V_0}{R_2}}_{= I_2} = 0$$

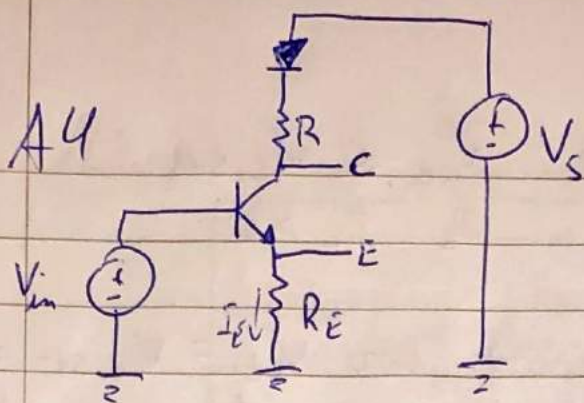
$$\Rightarrow \frac{V_{ref} - V_{in} - V_{ref}}{R_1} - \frac{V_{in} + V_{ref} - V_0}{R_2} = 0 \quad (\Rightarrow)$$

$$\frac{V_0}{R_2} = \frac{V_{in}}{R_1} + \frac{V_{in}}{R_2} + \frac{V_{ref}}{R_2} \quad (\Rightarrow) \quad V_0 = \left(1 + \frac{R_2}{R_1}\right) V_{in} + V_{ref}$$

$$V_0 = 3V_{in} + V_{ref} = 11 \text{ V}$$

$$I_2 = \frac{V_A - V_0}{R_2} = \frac{V_{in} + V_{ref} - V_0}{R_2} = \frac{V_{in} + V_{ref} - 3V_{in} - V_{ref}}{R_2} = -\frac{2V_{in}}{R_2}$$

$$= -6 \text{ A} = -20 \text{ mA}$$



a)

$$V_{in} - V_E = V_{BE, SAT} \quad (\Rightarrow) \quad V_E = V_{in} - V_{BE, SAT} = 5V$$

$$I_E = \frac{V_E}{R_E} = \frac{5}{50} = 100 \text{ mA}$$

$$I_C \approx I_E - I_B \approx I_E = 100 \text{ mA}$$

$$\text{K.V.L.: } V_S - V_D - R I_C - V_{CE} - V_E = 0$$

$$\begin{aligned} (\Rightarrow) V_{CE} &= V_S - V_D - V_E - \frac{R}{R_E} V_E \\ &= 24 - 2 - 5 - \frac{100}{50} \times 5 = 24 - 17 = 7V \end{aligned}$$

$$I_B = \frac{1}{\beta} I_C = \frac{100 \text{ mA}}{300} = \frac{1}{3} \text{ mA} = 333 \mu A$$

$\therefore I_B > 0, I_C > 0, V_{CE} > V_{CE, SAT} \Rightarrow \text{Active region}$

$$R_E = ?$$

A4.b) Saturation mode: $V_{CE} \leq V_{CE, SAT}$
 $I_B, I_C > 0$

Let us analyze the circuit for $V_{CE} = V_{CE, SAT} = 0.2 \text{ V}$
(border between the saturation and active regions)

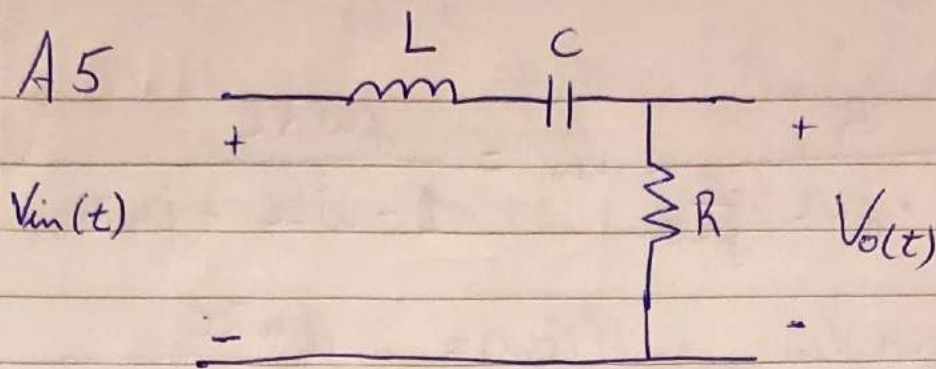
From A4.a): $I_C \approx I_E = \frac{5}{R_E}$

KVL: $V_S - V_D - R I_C - V_{CE} - V_E = 0 \quad (=)$

$$\frac{5 R}{R_E} = 24 - 2 - 0.2 - 5 \quad (=) \quad R_E = \frac{500}{16.8} \approx 29.7 \Omega$$

$R_E = 29.7 \Omega$ is the largest value for which the BJT is in Saturation.

✓ + A larger R_E than 29.7Ω will decrease $I_E = \frac{5}{R_E}$, decrease $I_C \approx I_E$, which will make V_{CE} increase above $V_{CE, SAT}$ so that the KVL holds (note that, in the KVL, V_S , V_D , and V_E are constant, so only I_C and V_{CE} can vary).



$$V_{in}(t) = 3 \sin\left(10^4 \pi t + \frac{\pi}{2}\right) ; \quad V_o(t) = ?$$

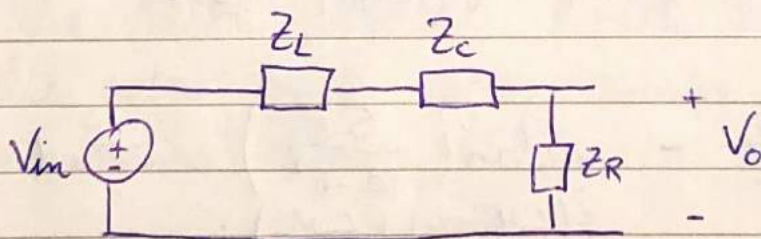
$$\omega = 10^4 \pi \text{ rad/s}$$

i) Associate $V_{in}(t)$ to a varying complex voltage
 $V_{in}(t) = \text{Im}(V_{cin}(t)) ; \quad V_{cin}(t) = 3 \cos(10^4 \pi t + \frac{\pi}{2}) + j 3 \sin(10^4 \pi t + \frac{\pi}{2})$

In polar form: $V_{cin}(t) = 3 e^{j(10^4 \pi t + \frac{\pi}{2})}$

$$= \underbrace{3 e^{j\frac{\pi}{2}}}_{= V_{in}} \times e^{j\omega t} = V_{in} \times e^{j\omega t}$$

For AC analysis, we convert the AC circuit to a DC circuit with constant complex-valued voltages and complex impedances:



where $V_{in} = 3 e^{j\frac{\pi}{2}}$, $V_o = ?$, $Z_R = R$, $Z_L = j\omega L$, $Z_C = \frac{1}{j\omega C}$

From KVL, we get:

$$V_o = \frac{Z_R}{Z_R + Z_L + Z_C} V_{in}$$

A5 (cont.)

$$V_o = \frac{R}{R + j\omega L + \frac{1}{j\omega C}} V_{in} = \frac{j\omega RC}{1 - \omega^2 LC + j\omega RC} V_{in}$$

$$V_o = H(j\omega) V_{in} \quad ; \quad H(j\omega) = \frac{j\omega RC}{1 - \omega^2 LC + j\omega RC}$$

$$\omega = 10^4 \pi \text{ rad/s}$$

$$R = 50 \Omega, \quad C = 10^{-6} \text{ F}, \quad L = 10^{-3} \text{ H}$$

$$\begin{aligned} H(j10^4 \pi) &= \frac{j \cdot 10^4 \cdot \pi \cdot 50 \cdot 10^{-6}}{1 - 10^8 \cdot \pi^2 \cdot 10^{-9} + j \cdot 10^4 \cdot \pi \cdot 50 \cdot 10^{-6}} \\ &= \frac{j 5\pi \times 10^{-1}}{1 - 10^{-1} \pi^2 + j 5\pi \times 10^{-1}} = \frac{j 5\pi}{10 - \pi^2 + j 5\pi} \end{aligned}$$

To solve $V_o = H(j\omega) V_{in}$, we need to convert $H(j\omega)$ into polar form: $H(j\omega) = |H(j\omega)| \times e^{j\angle H(j\omega)}$

$$|H(j10^4 \pi)| = \frac{|j 5\pi|}{|10 - \pi^2 + j 5\pi|} = \frac{5\pi}{\sqrt{(10 - \pi^2)^2 + (5\pi)^2}}$$

$$\angle H(j10^4 \pi) = \frac{\pi}{2} - \arctan\left(\frac{5\pi}{10 - \pi^2}\right) \text{ rad}$$

$$\begin{aligned} V_o &= |H(j10^4 \pi)| \cdot |V_{in}| \times e^{j(\angle H(j10^4 \pi) + \angle V_{in})} \\ &= \frac{15\pi}{\sqrt{(10 - \pi^2)^2 + 25\pi^2}} \times e^{j\left(\pi - \arctan\left(\frac{5\pi}{10 - \pi^2}\right)\right)} \end{aligned}$$

(A5 cont. 2)

$$V_{co}(t) = V_0 \times e^{j10^4 \pi t} \Rightarrow V_0(t) = \text{Im}(V_{co}(t))$$

$$V_0(t) = |V_0| \sin(10^4 \pi t + \angle V_0)$$

$$= \frac{15 \pi}{\sqrt{(10 - \pi^2)^2 + 25 \pi^2}} \sin\left(10^4 \pi t + \pi - \arctan\left(\frac{5 \pi}{10 - \pi^2}\right)\right)$$

To determine the type of filter, we look at $H(j\omega)$ and how it varies with ω .

$$|H(j0)| = \frac{0}{1} = 0$$

$$\lim_{\omega \rightarrow \infty} |H(j\omega)| = \lim_{\omega \rightarrow \infty} \left| \frac{j\omega RC}{1 - \omega^2 LC + j\omega RC} \right| =$$

$$\approx \lim_{\omega \rightarrow \infty} \left| \frac{j\omega RC}{-\omega^2 LC} \right| = \lim_{\omega \rightarrow \infty} \frac{|jR|}{|- \omega L|} = 0$$

The filter blocks both the very low and the very high frequencies, so it is a Band-Pass filter.