# Thematic Ranking of Object Summaries for Keyword Search DKE 2018

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# Outline

# 1. Motivation

- 2. Background & Related work
- 3. Themtiac Size-l OSs
- 4. Approaches
- **5. Evaluation Results**

6. Conclusion & Future Work

- Relational Databases are everywhere: Web, Desktops etc.
- Social graphs are also everywhere!
- Difficult to retrieve information about a Data Subject (DS) unless you know very well:
  - $\circ$  **SQL** and
  - Schema details etc.
- There is a need for keyword search facilities analogous to Web



#### Select \*

From Employees, Orders, Shippers
Where Employees.ID=Orders.ID
AND Orders.Shipper=Shippers.ID
AND Name="Leverling"

#### Query Search: **Faloutsos** Web Search Result: ranked set of links and snippets



#### Query Search: **Faloutsos** Web Search Result: ranked set of links and snippets



Current Position: Professor.

Courtesy appointment: Electrical and Computer Engineering, CMU

Query Search: FaloutsosQuery Search: FaloutsosWeb Search Result: ranked set of linksOS Result: set of OSs and size-l OSs.and snippetsOS Result: set of OSs and size-l OSs.



**Object** Summaries (OS)

About OSs - About Demo - People - Publications

Query Search: FaloutsosQuery Search: FaloutsosWeb Search Result: ranked set of linksOS Result: set of OSs and size-l OSs.and snippetsOS Result: set of OSs and size-l OSs.

Faloutsos	<u> </u>	
About 305,000 mults (0.29 seconds)	•	Object
Christos Faloutsos - School of Comput	ter Science - Carnegie Mellon	Summaries (OS)
12 Sep 2011 - SCS CSD Professor's affiliatons teaching.	, research, projects, publications and	A Novel Keyword Search Paradigm in Relational Databases
Publications/patents - Courses - Talks/tutoria	Is - Researchers Developing	DBLP • Taloutsos Search Atounced Jearch Advanced Jearch Advanc
Christos Faloutsos www.cs.cmu.edu/-christos/publications.html 2002 Performance - best student paper award: and Christos Faloutsos, Capturing the spatio-4	Mengzhi Wang, Anastasala Allamaki emporal behavior of real	
Petros Faloutsos, Ph.D. www.cs.ucla.edu/~pfal/ Assistant Professor of Computer Science, Direc	ctor and Founder of THE M.A.Gix Lab.	
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University of California, Los Angeles. Departme + Interfaces - Motion Control - Facial Animation [Publications/patents] [Software] [ U.S. mail add Christos F Deta. of C Compose Vision For Pittsburgh, Admin: Mary 112-268. email [frst	Talks/tutorials] [Courses] [Service] [Misc.] ress: aloutsos computer Science, GHC 8019 Melon University per Avenue .PA 15213-3891 m Walgora 1505, GHC 8120 simital-and-her-last-name] AT cs DOT cmm DOT edu	About OSa - About Demo - People - Publications         Object Summaries (OS) Christos Faloutsos         DBLP: search for Christos Faloutsos         Author: Christos Faloutsos         Author: Christos Faloutsos         Conference: Calculated         Conference: Storage and Retirout for Image and Video Databases (SPIE) 1993         Conference: Storage and Retirout for Image and Video Databases (SPIE) 1993         Conference: ACM DL 1997         Conference: ACM DL 1997         Conference: ACM DL 1997         Calculate Storage Concenter Storage         Conference: ACM DL 1997         Calculate Storage Concenter Storage
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#### KW-ID = "Janet Leverling"





- t<sup>DS</sup> a central tuple containing the Kw; tuples around t<sup>DS</sup> contain additional information about the Data Subject.
- **R**<sup>DS</sup> the corresponding central Relation; similarly Relations around contain additional information.



CustomerCustomerDemo

KW-ID = "Janet Leverling"

Orders

Shippers

Customers

Order Details



CustomerDemographics

Suppliers

Products |

Categories

- t<sup>DS</sup> a central tuple containing the Kw; tuples around t<sup>DS</sup> contain additional information about the Data Subject.
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KW-ID = "Janet Leverling"

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- **R**<sup>DS</sup> the corresponding central Relation; similarly Relations around contain additional information.

[Fakas, DKE, 2011]



#### **OS for "Janet Leverling"** - EmployeeID LastName FirstName Title Iddress PostalCode ---Leverling Janet Sales Representative 722 Moss Bay Blvd. 98033 ... (e<sub>3</sub>) Employees (Reports To) LastName FirstName Fuller Andrew (e<sub>2</sub>) Territories, Region TerritoryDescription RegionDescription Southern (et1, t4, r2) Atlanta Orders OrderID ShinName ShinAddress OrderDate RequiredDate ShinnedDate 10273 QUICK-Stop Taucherstraße 10 1996-08-05 1996-09-02 0( 1996-08-12 (02) Customers CompanyName ContactName QUICK-Stop Margaret Peacock (C2) Shippers CompanyName Federal Shipping(S3) Order Details UnitPrice Quantity Discount (od₁) 15.2000 50 0.2 Products - ProductName QuantityPerUnit Chang 24 - 12 oz bottles (p2) Categories CategoryName Description (ca₁) Beverages Soft drinks, coffees, teas, beers, ...

# **2.3 Motivation** *Ranking of Size-l OSs*

Query: identifying keyword: Chen

For the DBLP dataset, there 1,982 OSs, i.e. 1,982 authors having the name "Chen".

Using Authoritative ranking, Peter Chen will always be ranked first because of his many citations. This is ineffective for users who search for a DS that does not have the best importance scores.

In view of this, in this paper, we propose the thematic ranking of OSs, where thematic keywords are also input by the user.

### 2.3 Motivation Thematic Ranking of Size-l OSs Query: identifying keyword: Chen thematic keyword: Mining the additional thematic keyword makes 'Ming-Syan Chen' previal, since his OS contains 'Mining' many times.

Author: Ming-Syan Chen [1.00, 0.45]
Paper: A robust and efficient clustering algorithm based
Co-Author: Cheng-Ru Lin. Conf.: KDD. Year: 2002
Paper: Distributed data <i>mining</i> in a chain store [0.98, 0.16]
Co-Author: Philip S. Yu, Conf.: KDD. Year: 2002.
Paper: Mining Relationship between Triggering[0.98, 0.15]
Co-Author: Philip S. Yu, Conf.: SDM. Year: 2002.
Paper: DOMISA: DOM-Based infor Mining [0.98, 0.18]
Co-Author: Hung-Yu Kao, Conf.: SDM, Year: 2004.
Paper: Efficient Mining for Association Rules[0.98, 0.19]
Co-Author: Philip S. Yu, Conf.: CIKM Year: 1995.
Cited by: Parallel <i>Mining</i> of Association [0.93, 0.36]
Cited by: Data Mining: An Overview from [0.93, 0.82]
Cited by: Dynamic Load Balan Mining [0.93, 0.16]
Cited by: Parallel Mining Algorithms for G [0.93, 0.16]

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# 3 Themtiac Size-l OSs

Author: Ming-Syan Chen [1.00, 0.45] Paper: A robust and efficient clustering algorithm based ... Co-Author: Cheng-Ru Lin. Conf.: KDD. Year: 2002 Paper: Distributed data *mining* in a chain store... [0.98, 0.16] Co-Author: Philip S. Yu, ... Conf.: KDD. Year: 2002. Paper: Mining Relationship between Triggering...[0.98, 0.15] Co-Author: Philip S. Yu, ... Conf.: SDM. Year: 2002. Paper: DOMISA: DOM-Based infor... Mining... [0.98, 0.18] Co-Author: Hung-Yu Kao, ... Conf.: SDM, Year: 2004. Paper: Efficient ... Mining for Association Rules. [0.98, 0.19] Co-Author: Philip S. Yu, ... Conf.: CIKM Year: 1995. Cited by: Parallel Mining of Association ... [0.93, 0.36]Cited by: Data Mining: An Overview from... [0.93, 0.82] Cited by: Dynamic Load Balan.. Mining... [0.93, 0.16] Cited by: Parallel *Mining* Algorithms for G... [0.93, 0.16]

#### **Definition:**

A query Q comprises two sets of keywords,  $Q = \langle q_1, q_2 \rangle$ ,

- $q_1$  is a set of identifying keywords
- $q_2$  is a set of thematic keywords

#### **Criterias:**

- 1. global Importance;
- 2. IR-properties; and
- **3**. Affinity

## 3 Themtiac Size-l OSs

Author: Ming-Syan Chen [1.00, 0.45] Paper: A robust and efficient clustering algorithm based ... Co-Author: Cheng-Ru Lin. Conf.: KDD. Year: 2002 Paper: Distributed data *mining* in a chain store... [0.98, 0.16] Co-Author: Philip S. Yu, ... Conf.: KDD. Year: 2002. Paper: Mining Relationship between Triggering...[0.98, 0.15] Co-Author: Philip S. Yu, ... Conf.: SDM. Year: 2002. Paper: DOMISA: DOM-Based infor... Mining... [0.98, 0.18] Co-Author: Hung-Yu Kao, ... Conf.: SDM, Year: 2004. Paper: Efficient ... Mining for Association Rules. [0.98, 0.19] Co-Author: Philip S. Yu, ... Conf.: CIKM Year: 1995. [0.93, 0.36]Cited by: Parallel Mining of Association... Cited by: Data Mining: An Overview from... [0.93, 0.82] Cited by: Dynamic Load Balan.. Mining ... [0.93, 0.16]Cited by: Parallel *Mining* Algorithms for G... [0.93, 0.16]

$$score_1(O, q_1) = Im(t^{DS}),$$

where

$$score_2(O, q_2) = \frac{\sum_{t \in O} s(t, q_2)}{1 - \alpha + \alpha \cdot \frac{dl(O)}{avdl(OS)}}$$

$$score(O, Q) = score_1(O, q_1) \cdot score_2(O, q_2)$$

#### **Definition:**

A query Q comprises two sets of keywords,  $Q = \langle q_1, q_2 \rangle$ ,

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#### **Criterias:**

- 1. global Importance;
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$$s(t, q_2) = \sum_{w \in t \cap q_2} \left(1 + \ln(1 + \ln(tf_w(t)))) \cdot \ln(idf_w) \cdot li(t),\right)$$

$$idf_w = \frac{N_{OS} + 1}{df_w(OS)},$$

$$li(t) = Af(t) \cdot Im(t).$$

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## **4.1 Problem reformulation**

We reformulate our OSs ranking problem as a *top-k* Group By join problem (*k*GBJ).

Considering two selection operations on  $R^{DS}$  and  $R^{TH}$  then we get  $R^{DS}(q_1)$  and  $R^{TH}(q_2)$ 



Identifying Keywords $(q_1)$	Frequency in DBLP
David	4,235
Chen	1,982
Wang	1,778
Alan	660
John	3,717
Nick	179
Thematic Keywords $(q_2)$	Frequency in DBLP
Mining	2,961
System	32,253
Logic	65
Data	22,500

# **4.1 Baseline: Bi-Directional approach** *BD approach*

As in a query optimizer, given the sizes of  $R^{DS}(q_1)$  and  $R^{TH}(q_2)$ , the estimation of the optimal meeting point is done with the help of statistics.



**Meeting point Examples** 

# **4.2 Top-k Bi-Directional approach** *kBD approach*

Rationale of this approach is to avoid the entire BD traversal and processing of our input (i.e. of  $R^{DS}(q_1)$  and  $R^{TH}(q_2)$ ).

We achieves this by estimating **upper** and **lower bounds** for each OS and by managing them in descending order of their upper bounds in a max-heap.

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# **5. Experimental Evaluation** *Effectiveness*

k	Precision(=Recall)	Ranking Correlation
5	02.0%	0.84
10	06 507	0.09
10	90.5%	0.92
15	98.8%	0.96
20	100%	0.98
25	100%	0.99

**Precision(Recall) and Ranking Correlation** 

# **5. Experimental Evaluation** *Efficiency*



Efficiency of *BD* and *kBD* for Various Values of *k* 

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# **6.1 Conclusion & Future Work** *Contributions*

• The formal definition of *thematic ranking object summaries* for keyword search.

• The an efficient *top-k group-by join* algorithm.

• Applications: Google, Google Desktop, DBMS, etc.

Thematic Ranking of Object Summaries for Keyword Search

Thank you

**Questions!** 

# **4.2 Top-k Bi-Directional approach** *kBD approach*

Upper and lower bounds of OSs are calculated as follows:

 $LB(O) = In(O) \cdot \sum_{j=1}^{l} n_j \cdot s(t_j)$  $UB_1(O, Q) = LB(O) + In(O) \cdot (M - \sigma) \cdot s(t_{l+1})$ 

 $\gamma = \min\{m \cdot (|R^{\mathrm{Th}}(q_2)| - l), M - \sigma\}$  $UB_2(O, Q) = LB(O)) + In(O) \cdot \left(\sum_{j=1}^d s(t_{l+j}) \cdot m + s(t_{l+d+1}) \cdot r\right) d = \lfloor \gamma/m \rfloor \quad r = \gamma \mod m$ 

**further tighten**  
$$UB_{3}(O, Q) = LB(O) + In(O) \cdot \left(\sum_{j=1}^{d} m \cdot s(t_{a_{j}}) + r \cdot s(t_{a_{d+1}})\right)$$

# **4.2 Top-k Bi-Directional approach**

**Calculating the Upper Bound Scores of** 

an OS O(In(O) = 1.0, M = 13, m = 4)

Algorithm 1. kBD Algorithm

 $R^{\text{TH}}$  $R^{\text{TH}}$  $R^{\text{TH}}$ **kBD** ( $R^{DS}(q_1), R^{Th}(q_2), k$ ) tuple tuple tuple  $s(\cdot)$  $s(\cdot)$  $s(\cdot)$  $H := \emptyset;$ 1: 0.90.90.9 $t_1$  $t_1$  $t_1$ 2:  $L^{\mathrm{Th}} := R^{\mathrm{Th}}(q_2);$ 0.8 0.8 $t_2$  $t_2$  $t_2$ 0.8tDS 0.7 0.7 $t_3$ +DS  $t_3$  $t_3$ 0.73: sort tuples in  $L^{\text{Th}}$  in descending order of their  $s(\cdot)$  scores; 0.50.5 $t_4$ 0.5 $t_4$  $t_4$ 4: for each Q w.r.t.  $t^{DS}$  in  $R^{DS}(q_1)$  do  $t_5$ 0.5 $t_5$ 0.5 $t_5$ 0.55: LB(O) := 0; UB(O) := CALCUB O;0.30.3 $t_6$  $t_6$  $t_6$ 0.3insert O into H with priority UB(O); 6:  $t_7$ 0.20.20.2 $t_7$  $t_7$ 7: while  $k > 0 \land H$  is not empty do  $t_8$ 0.2 $t_8$ 0.2 $t_8$ 0.28: pop  $Q_{cur}$  from H; (a)  $UB_1(\mathcal{O}) = 10.6$ (b) UB'<sub>1</sub>(𝒫)=9.6 (c)  $UB_2(\mathcal{O})=9.3$  $\mathcal{O}_{next} := H.top();$ 9:  $R^{\text{TH}}$  $R^{\text{TH}}$  $R^{\text{TH}}$ 10: if  $LB(\mathcal{O}_{cur}) \geq UB(\mathcal{O}_{next})$  then tuple tuple tuple  $s(\cdot)$  $s(\cdot)$  $s(\cdot)$ report  $O_{cur}$  as a result; 11: 0.90.9 $t_1$ 0.9 $t_1$  $t_1$ k = k - 1;12:0.80.80.8 $t_2$  $t_2$  $t_2$ 13: else 0.70.7 $t_3$ +DS  $t_3$  $t_3$ 0.714:  $t_i$ := the next tuple in  $L^{\text{Th}}$  can join with  $Q_{cur}$ ; 0.50.5 $t_4$  $t_4$  $t_4$ 0.5tDS 15:  $n := \text{JOIN } O_{cur}, t_i;$ 0.50.5 $t_5$  $t_5$  $t_5$ 0.516:  $LB(O_{cur}) := LB(O_{cur}) + n \cdot In(O_{cur}) \cdot s(t_l, q_2);$ 0.30.30.3 $t_6$  $t_6$  $t_6$ 17:  $UB(O_{cur}) := CALCUB O_{cur};$  $t_7$ 0.20.20.2 $t_7$  $t_7$ 0.2push  $O_{cur}$  back into H with priority  $UB(O_{cur})$ ;  $t_8$  $t_8$ 0.2 $t_8$ 0.218: (d) UB<sub>2</sub>(𝔅)=8.4 (f) UB<sub>2</sub><sup>'</sup>(𝔅)=6.2 (e) UB<sub>3</sub>(𝔅)=7.6

# **4.2 Top-k Bi-Directional approach**

#### Algorithm 1. kBD Algorithm

**kBD**  $(R^{\text{DS}}(q_1), R^{\text{Th}}(q_2), k)$  $H := \emptyset;$ 1: 2:  $L^{\mathrm{Th}} := R^{\mathrm{Th}}(q_2);$ 3: sort tuples in  $L^{\text{Th}}$  in descending order of their  $s(\cdot)$  scores; 4: for each Q w.r.t.  $t^{DS}$  in  $R^{DS}(q_1)$  do 5: LB(O) := 0; UB(O) := CALCUB O;insert O into H with priority UB(O); 6: 7: while  $k > 0 \land H$  is not empty do 8: pop  $Q_{cur}$  from H;  $\mathcal{O}_{next} := H.top();$ 9: 10: if  $LB(\mathcal{O}_{cur}) \geq UB(\mathcal{O}_{next})$  then 11: report  $Q_{cur}$  as a result; k = k - 1;12:13: else  $t_i$ := the next tuple in  $L^{\text{Th}}$  can join with  $O_{cur}$ ; 14: 15:  $n := \text{JOIN } O_{cur}, t_l;$ 16:  $LB(\mathcal{O}_{cur}) \coloneqq LB(\mathcal{O}_{cur}) + n \cdot In(\mathcal{O}_{cur}) \cdot s(t_l, q_2);$ 17:  $UB(O_{cur}) := CALCUB O_{cur};$ 

18: push  $O_{cur}$  back into H with priority  $UB(O_{cur})$ ;

#### The kBD Algorithm for k = 1

	OS	UB(.)	LB(.)	
	$\mathcal{O}_1$	8.0	0	
	$\mathcal{O}_2$	6.0	0	
	$\mathcal{O}_3$	10.0	0	
	$\mathcal{O}_4$	5.0	0	
	$\mathcal{O}_5$	4.0	0	
	(	a) Initiali	zation	
	OS	UB(.)	LB(.)	
[	OS	<i>UB</i> (.)	<i>LB</i> (.)	
	OS $\mathcal{O}_1$	UB(.) 7.5	<i>LB</i> (.) 5.0	
	OS $\mathcal{O}_1$ $\mathcal{O}_2$	UB(.) 7.5 6.0	<i>LB</i> (.) 5.0 0	
	OS $O_1$ $O_2$ $O_3$	UB(.) 7.5 6.0 7.0	LB(.) 5.0 0 6.5	
	$\begin{array}{c} OS \\ \mathcal{O}_1 \\ \mathcal{O}_2 \\ \mathcal{O}_3 \\ \mathcal{O}_4 \end{array}$	UB(.) 7.5 6.0 7.0 5.0	LB(.) 5.0 0 6.5 0	
	$\begin{array}{c} OS \\ \mathcal{O}_1 \\ \mathcal{O}_2 \\ \mathcal{O}_3 \\ \mathcal{O}_4 \\ \mathcal{O}_5 \end{array}$	UB(.) 7.5 6.0 7.0 5.0 4.0	LB(.) 5.0 0 6.5 0 0	

OS	UB(.)	LB(.)				
$\mathcal{O}_1$	8.0	0				
$\mathcal{O}_2$	6.0	0				
$\mathcal{O}_3$	7.0	6.5				
$\mathcal{O}_4$	5.0	0				
$\mathcal{O}_5$	4.0	0				
$ \begin{array}{c} H = \langle \mathcal{O}_1, \mathcal{O}_3, \mathcal{O}_2, \mathcal{O}_4, \mathcal{O}_5 \rangle \\ \mathcal{O}_{cur} = \mathcal{O}_1, \ \mathcal{O}_{next} = \mathcal{O}_3 \\ \text{(b) Iteration 1} \end{array} $						
OS	UB(.)	LB(.)				
0	6.0	0.0				

OS	UB(.)	LB(.)							
$\mathcal{O}_1$	6.2	6.0							
$\mathcal{O}_2$	6.0	0							
$\mathcal{O}_3$	7.0	6.5							
$\mathcal{O}_4$	5.0	0							
$\mathcal{O}_5$	4.0	0							
$H = \langle \mathcal{C} \\ \mathcal{O}_{cur} =$	$ \begin{array}{c c} \hline \mathcal{O}_5 & 4.0 & 0 \\ \hline H = \langle \mathcal{O}_3, \mathcal{O}_1, \mathcal{O}_2, \mathcal{O}_4, \mathcal{O}_5 \rangle, \\ \mathcal{O}_{cur} = \mathcal{O}_3, \mathcal{O}_{next} = \mathcal{O}_1 \\ \text{(d) Iteration 3} \end{array} $								

### **4.3 Multiple thematic relations** *Holistic Top-k BD (HkBD) algorithm*

Given j thematic relations  $R_1^{Th}$ , ...,  $R_j^{Th}$ , we can extend analogously the original *k*BD algorithm by defining appropriate upper and lower bound scores for each *DS*. We can easily see that the sum of the upper (resp. lower) bound scores of all join paths (denote as *JP*) is the upper (resp. lower) bound score of an OS, namely:

$$UB^{H}(O, Q) = \sum_{\mathcal{JP}_{i}} UB^{\mathcal{JP}_{i}}(O, Q),$$
$$LB^{H}(O, Q) = \sum_{\mathcal{JP}_{i}} LB^{\mathcal{JP}_{i}}(O, Q),$$

where  $JP_i$  ranges over all thematic paths and  $UB^{JPi}(.)$  (resp. $UB^{JPi}(.)$ ) is the upper (resp. lower) bound score of O.

# **4.3 Multiple thematic relations** *Holistic Top-k BD (HkBD) algorithm*

We force the meeting point to the common *G*<sup>DS</sup> prefix which is shared by all paths, then we can compute the join result once and reuse if later for the other paths;

*HkBD* approach is advantageous in this aspect over the *HBD* algorithm, as it facilitates reuse of join results.



#### **Examples of Join Paths**