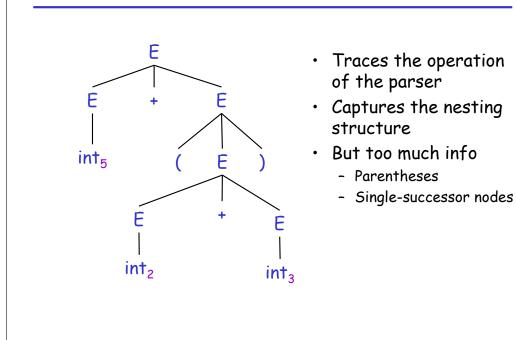
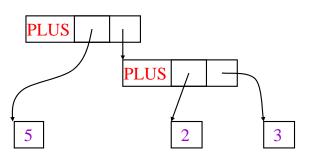
	Review of Parsing			
Abstract Syntax Trees & Top-Down Parsing	 Given a language L(G), a parser consumes a sequence of tokens s and produces a parse tree Issues: How do we recognize that s ∈ L(G)? A parse tree of s describes how s ∈ L(G) Ambiguity: more than one parse tree (possible interpretation) for some string s Error: no parse tree for some string s How do we construct the parse tree? 			
Abstract Syntax Trees	Abstract Syntax Trees (Cont.)			
 So far, a parser traces the derivation of a sequence of tokens The rest of the compiler needs a structural representation of the program Abstract syntax trees 	 Consider the grammar E → int (E) E + E And the string 5 + (2 + 3) After lexical analysis (a list of tokens) 			
 Like parse trees but ignore some details Abbreviated as AST 	int ₅ '+' '(' int ₂ '+' int ₃ ')'			

Example of Parse Tree



Example of Abstract Syntax Tree



- Also captures the nesting structure
- But <u>abstracts</u> from the concrete syntax
 → more compact and easier to use
- An important data structure in a compiler

Semantic Actions

- This is what we will use to construct ASTs
- Each grammar symbol may have <u>attributes</u>
 - An attribute is a property of a programming language construct
 - For terminal symbols (lexical tokens) attributes can be calculated by the lexer
- Each production may have an action
 - Written as: $X \rightarrow Y_1 \dots Y_n$ { action }
 - That can refer to or compute symbol attributes

Semantic Actions: An Example

Consider the grammar

 $E \rightarrow int \mid E + E \mid$ (E)

6

8

- For each symbol X define an attribute X.val
 - For terminals, val is the associated lexeme
 - For non-terminals, val is the expression's value (which is computed from values of subexpressions)
- We annotate the grammar with actions:
 - $\begin{array}{ll} \mathsf{E} \rightarrow \mathsf{int} & \{ \ \mathsf{E}.\mathsf{val} = \mathsf{int}.\mathsf{val} \ \} \\ & | \ \mathsf{E}_1 + \mathsf{E}_2 & \{ \ \mathsf{E}.\mathsf{val} = \mathsf{E}_1.\mathsf{val} + \mathsf{E}_2.\mathsf{val} \ \} \\ & | \ (\ \mathsf{E}_1 \) & \{ \ \mathsf{E}.\mathsf{val} = \mathsf{E}_1.\mathsf{val} \ \} \end{array}$

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Semantic Actions: An Example (Cont.)

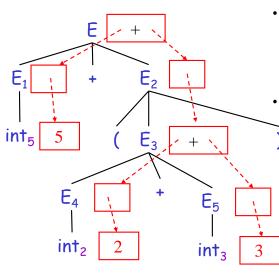
- String: 5 + (2 + 3)
- Tokens: int₅ '+' '(' int₂ '+' int₃ ')'

<u>Productions</u>	<u>Equations</u>
$E \rightarrow E_1 + E_2$	E.val = E ₁ .val + E ₂ .val
$E_1 \rightarrow int_5$	E ₁ .val = int ₅ .val = 5
$E_2 \rightarrow (E_3)$	E_2 .val = E_3 .val
$E_3 \rightarrow E_4 + E_5$	$E_3.val = E_4.val + E_5.val$
$E_4 \rightarrow int_2$	$E_4.val = int_2.val = 2$
$E_5 \rightarrow int_3$	$E_5.val = int_3.val = 3$

Semantic Actions: Dependencies

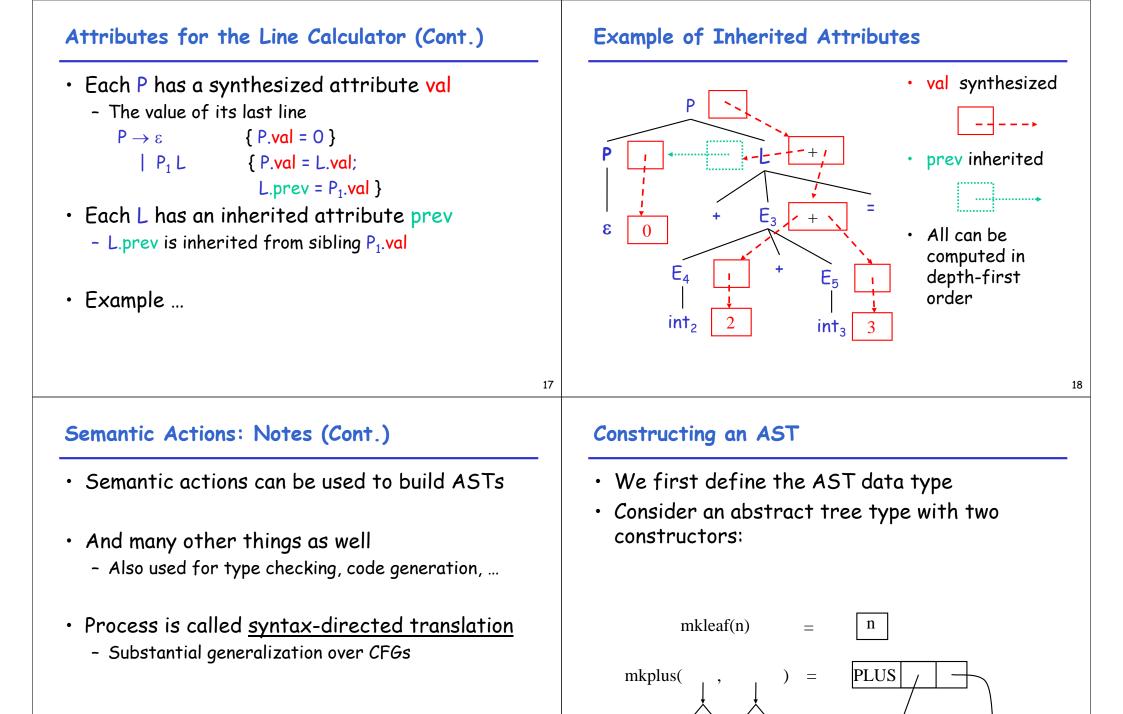
Semantic actions specify a system of equations - Order of executing the actions is not specified • Example: E_3 , val = E_4 , val + E_5 , val - Must compute E_4 .val and E_5 .val before E_3 .val - We say that E_3 , val depends on E_4 , val and E_5 , val • The parser must find the order of evaluation 10 **Evaluating Attributes**

Dependency Graph



- Each node labeled with a non-terminal E has one slot for its val attribute
- Note the dependencies
- An attribute must be computed after all its successors in the dependency graph have been computed
 - In the previous example attributes can be computed bottom-up
- Such an order exists when there are no cycles
 Cyclically defined attributes are not legal

Semantic Actions: Notes (Cont.)	Inherited Attributes				
 Synthesized attributes Calculated from attributes of descendents in the parse tree E.val is a synthesized attribute Can always be calculated in a bottom-up order Grammars with only synthesized attributes are called <u>S-attributed</u> grammars Most frequent kinds of grammars 	 Another kind of attributes Calculated from attributes of the parent node(s) and/or siblings in the parse tree Example: a line calculator 				
A Line Calculator	Attributes for the Line Calculator				
 Each line contains an expression E→ int E + E Each line is terminated with the = sign L→ E = + E = In the second form, the value of evaluation of the previous line is used as starting value A program is a sequence of lines P→ ε PL 	 Each E has a synthesized attribute val Calculated as before Each L has a synthesized attribute val L → E = {L.val = E.val } I + E = {L.val = E.val + L.prev } We need the value of the previous line We use an inherited attribute L.prev 				

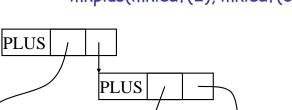


Constructing a Parse Tree

- We define a synthesized attribute ast
 - Values of ast values are ASTs
 - We assume that int.lexval is the value of the integer lexeme
 - Computed using semantic actions
 - $\begin{array}{ll} \mathsf{E} \rightarrow \mathsf{int} & \{ \mathsf{E}.\mathsf{ast} = \mathsf{mkleaf}(\mathsf{int.lexval}) \} \\ & | \ \mathsf{E}_1 + \mathsf{E}_2 & \{ \mathsf{E}.\mathsf{ast} = \mathsf{mkplus}(\mathsf{E}_1.\mathsf{ast}, \mathsf{E}_2.\mathsf{ast}) \} \\ & | \ (\mathsf{E}_1) & \{ \mathsf{E}.\mathsf{ast} = \mathsf{E}_1.\mathsf{ast} \} \end{array}$

Parse Tree Example

- Consider the string int₅ '+' '(' int₂ '+' int₃ ')'
- A bottom-up evaluation of the ast attribute:
 E.ast = mkplus(mkleaf(5), mkplus(mkleaf(2), mkleaf(3))



2

3

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Review of Abstract Syntax Trees

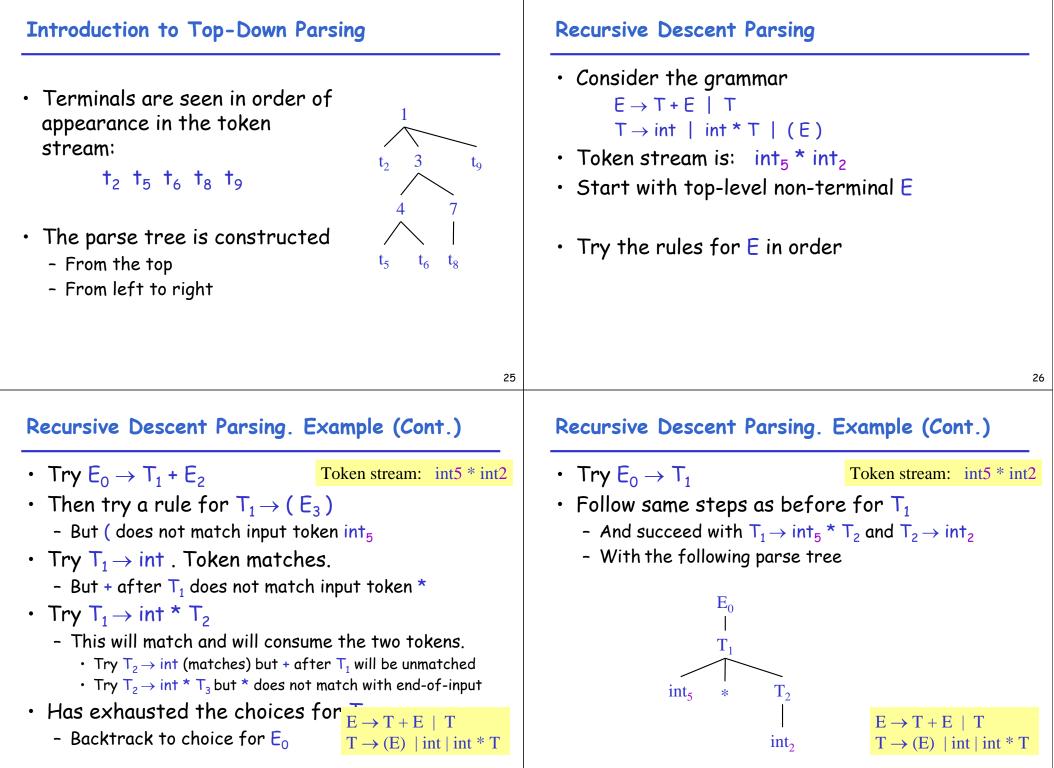
- We can specify language syntax using CFG
- A parser will answer whether $s \in L(G)$
- ... and will build a parse tree
- ... which we convert to an AST
- ... and pass on to the rest of the compiler
- Next two & a half lectures:
 - How do we answer $s \in L(G)$ and build a parse tree?
- After that: from AST to assembly language

Second-Half of Lecture 5: Outline

- Implementation of parsers
- Two approaches

5

- Top-down
- Bottom-up
- Today: Top-Down
 - Easier to understand and program manually
- Then: Bottom-Up
 - More powerful and used by most parser generators



Recursive Descent Parsing. Notes.

- Easy to implement by hand
- Somewhat inefficient (due to backtracking)
- But does not always work ...

When Recursive Descent Does Not Work

- Consider a production $S \rightarrow S$ a bool $S_1()$ { return S() && term(a); } bool S() { return $S_1()$; }
- S() will get into an infinite loop
- A left-recursive grammar has a non-terminal S \rightarrow^+ S α for some α
- Recursive descent does not work in such cases

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Elimination of Left Recursion

- Consider the left-recursive grammar $S \rightarrow S \alpha \mid \beta$
- S generates all strings starting with a β and followed by any number of $\alpha's$
- The grammar can be rewritten using rightrecursion

```
S \rightarrow \beta S'S' \rightarrow \alpha S' \mid \varepsilon
```

More Elimination of Left-Recursion

• In general

 $S \rightarrow S \alpha_1 \mid \dots \mid S \alpha_n \mid \beta_1 \mid \dots \mid \beta_m$

- All strings derived from S start with one of $\beta_{1,...,\beta_{m}}$ and continue with several instances of $\alpha_{1,...,\alpha_{n}}$
- Rewrite as

$$\begin{split} & \mathsf{S} \to \beta_1 \; \mathsf{S}' \; | \; \dots \; | \; \beta_{\mathsf{m}} \; \mathsf{S}' \\ & \mathsf{S}' \to \alpha_1 \; \mathsf{S}' \; | \; \dots \; | \; \alpha_{\mathsf{n}} \; \mathsf{S}' \; | \; \varepsilon \end{split}$$

General Left Recursion	Summary of Recursive Descent				
• The grammar $S \rightarrow A \alpha \mid \delta$ $A \rightarrow S \beta$ is also left-recursive because $S \rightarrow^{+} S \beta \alpha$	 Simple and general parsing strategy Left-recursion must be eliminated first but that can be done automatically Unpopular because of backtracking Thought to be too inefficient 				
 This left-recursion can also be eliminated 	 In practice, backtracking is eliminated by restricting the grammar 				
[See a Compilers book for a general algorithm]					
33	34				
Predictive Parsers	LL(1) Languages				
 Like recursive-descent but parser can "predict" which production to use By looking at the next few tokens No backtracking Predictive parsers accept LL(k) grammars L means "left-to-right" scan of input L means "leftmost derivation" k means "predict based on k tokens of lookahead" In practice, LL(1) is used 	 In recursive-descent, for each non-terminal and input token there may be a choice of production LL(1) means that for each non-terminal and token there is only one production Can be specified via 2D tables One dimension for current non-terminal to expand One dimension for next token A table entry contains one production 				

Predictive Parsing and Left Factoring

- Recall the grammar for arithmetic expressions $E \rightarrow T + E \mid T$ $T \rightarrow (E) \mid int \mid int * T$
- Hard to predict because
 - For T two productions start with int
 - For E it is not clear how to predict
- A grammar must be <u>left-factored</u> before it is used for predictive parsing

Left-Factoring Example

- Recall the grammar $\begin{array}{c|c} E \rightarrow T + E & | & T \\ T \rightarrow (E) & | & \text{int } | & \text{int } * T \end{array}$
- Factor out common prefixes of productions $E \rightarrow T X$ $X \rightarrow + E \mid \epsilon$ $T \rightarrow (E) \mid int Y$ $Y \rightarrow * T \mid \epsilon$

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LL(1) Parsing Table Example

- Left-factored grammar

• The LL(1) parsing table:

	int	*	+	()	\$
E	ТХ			ТΧ		
X			+ E		3	3
Т	int Y			(E)		
У		* T	3		3	3

LL(1) Parsing Table Example (Cont.)

- Consider the [E, int] entry
 - "When current non-terminal is E and next input is int, use production $\mbox{ E} \rightarrow \mbox{ T}\mbox{ X}$
 - This production can generate an int in the first place
- Consider the [Y,+] entry
 - "When current non-terminal is Y and current token is +, get rid of Y"
 - Y can be followed by + only in a derivation in which Y $\rightarrow~\epsilon$

LL(1) Parsing Tables: Errors

LL(1) I di sing i dbies: Li i di s	Using full sing fubles				
 Blank entries indicate error situations Consider the [E,*] entry "There is no way to derive a string starting with * from non-terminal E" 	 Method similar to recursive descent, except For each non-terminal S We look at the next token a And chose the production shown at [S,a] We use a stack to keep track of pending non-terminals We reject when we encounter an error state We accept when we encounter end-of-input 				
41	1	42			
LL(1) Parsing Algorithm	LL(1) Parsing Example				
	Stack Input Action	•			
initialize stack = <s \$=""> and next</s>	E\$ int*int\$ TX				

Using Parsing Tables

repeat case stack of

```
<X, rest> : if T[X,*next] = Y_1 \dots Y_n
then stack \leftarrow <Y_1 \dots Y_n rest>;
else error();
<t, rest> : if t == *next++
then stack \leftarrow <rest>;
else error();
until stack == <>
```

Stack	Input	Action					-	
E\$	int * int \$	ТХ						
TX\$	int * int \$	int Y						
int Y X \$	int * int \$	terminal						
Y X \$	* int \$	* Т						
* T X \$	* int \$	terminal						
TX\$	int \$	int Y						
int Y X \$	int\$	terminal						
Y X \$	\$	3						
X \$	\$	3						
\$	\$	ACCEPT						
1	1		int	*	+	()	\$
		t	TX		-	ТХ		
		2	X F		+ E	(5)	3	3
			Г int У			(E)		

*Τ ε

Constructing Parsing Tables Constructing Parsing Tables (Cont.) • LL(1) languages are those defined by a parsing • If $A \rightarrow \alpha$, where in the line of A we place α ? table for the LL(1) algorithm • In the column of t where t can start a string • No table entry can be multiply defined derived from α $-\alpha \rightarrow^* \dagger \beta$ - We say that $t \in First(\alpha)$ • We want to generate parsing tables from CFG • In the column of t if α is ε and t can follow an A - $S \rightarrow^* \beta A \dagger \delta$ - We say $t \in Follow(A)$ 45 46 **Computing First Sets** First Sets: Example Recall the grammar Definition $E \rightarrow T X$ $X \rightarrow + E \mid \varepsilon$ First(X) = { $t \mid X \rightarrow^* t\alpha$ } \cup { $\varepsilon \mid X \rightarrow^* \varepsilon$ } $Y \rightarrow * T \mid \varepsilon$ $T \rightarrow (E)$ | int Y Algorithm sketch • First sets 1. First(t) = { t } First(() = { (} First()) = {) } 2. $\epsilon \in First(X)$ if $X \to \epsilon$ is a production First(+) = {+} First(*) = {*} 3. $\varepsilon \in \text{First}(X)$ if $X \to A_1 \dots A_n$ First(int) = { int } and $\varepsilon \in \text{First}(A_i)$ for each $1 \le i \le n$ First(T) = { int, (} 4. First(α) \subseteq First(X) if X \rightarrow A₁ ... A_n α First(E) = { int, (} and $\varepsilon \in \text{First}(A_i)$ for each $1 \le i \le n$ First(X) = {+, ε } First(Y) = { *, ε }

Computing Follow Sets

Algorithm sketch Definition Follow(X) = { \dagger | S $\rightarrow^{*} \beta$ X $\dagger \delta$ } 1. $\$ \in Follow(S)$ 2. First(β) - { ε } \subset Follow(X) For each production $A \rightarrow \alpha \times \beta$ Intuition ٠ 3. Follow(A) \subset Follow(X) - If $X \rightarrow A B$ then First(B) \subset Follow(A) and $Follow(X) \subset Follow(B)$ For each production $A \rightarrow \alpha \times \beta$ where $\varepsilon \in \text{First}(\beta)$ - Also if $B \rightarrow^* \varepsilon$ then Follow(X) \subseteq Follow(A) - If S is the start symbol then $\$ \in Follow(S)$ 49 50 Follow Sets: Example Constructing LL(1) Parsing Tables • Recall the grammar Construct a parsing table T for CFG G $F \rightarrow T X$ $X \rightarrow + E \mid \varepsilon$ $Y \rightarrow * T \mid \varepsilon$ $T \rightarrow (E) \mid int Y$ • For each production $A \rightarrow \alpha$ in G do: Follow sets - For each terminal $t \in First(\alpha)$ do • T[A, \dagger] = α Follow(+) = { int, (} Follow(*) = { int, (} - If $\varepsilon \in \text{First}(\alpha)$, for each $t \in \text{Follow}(A)$ do Follow(() = { int, (} Follow(E) = {), \$ } • T[A, t] = α Follow(X) = { \$,) } Follow(T) = { +,) , \$ } - If $\varepsilon \in \text{First}(\alpha)$ and $\$ \in \text{Follow}(A)$ do Follow()) = $\{+, \}, \{+, \}$ Follow(\forall) = $\{+, \}, \{+, \}$ • T[A, \$] = α Follow(int) = { *, +,), \$ }

Computing Follow Sets (Cont.)

Notes on LL(1) Parsing Tables

- If any entry is multiply defined then G is not LL(1)
 - If G is ambiguous
 - If G is left recursive
 - If G is not left-factored
 - And in other cases as well
- Most programming language grammars are not LL(1)
- There are tools that build LL(1) tables

Review

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 For some grammars there is a simple parsing strategy

Predictive parsing

• Next time: a more powerful parsing strategy