Abstract Syntax Trees & Top-Down Parsing	 Review of Parsing Given a language L(G), a parser consumes a sequence of tokens s and produces a parse tree Issues: How do we recognize that s ∈ L(G)? A parse tree of s describes how s ∈ L(G) Ambiguity: more than one parse tree (possible interpretation) for some string s Error: no parse tree for some string s How do we construct the parse tree?
Abstract Syntax Trees	Compiler Design 1 (2011) Abstract Syntax Trees (Cont.)
 So far, a parser traces the derivation of a sequence of tokens The rest of the compiler needs a structural representation of the program <u>Abstract syntax trees</u> Like parse trees but ignore some details Abbreviated as AST 	 Consider the grammar E → int (E) E + E And the string 5 + (2 + 3) After lexical analysis (a list of tokens) int₅ '+' '(' int₂ '+' int₃ ')' During parsing we build a parse tree

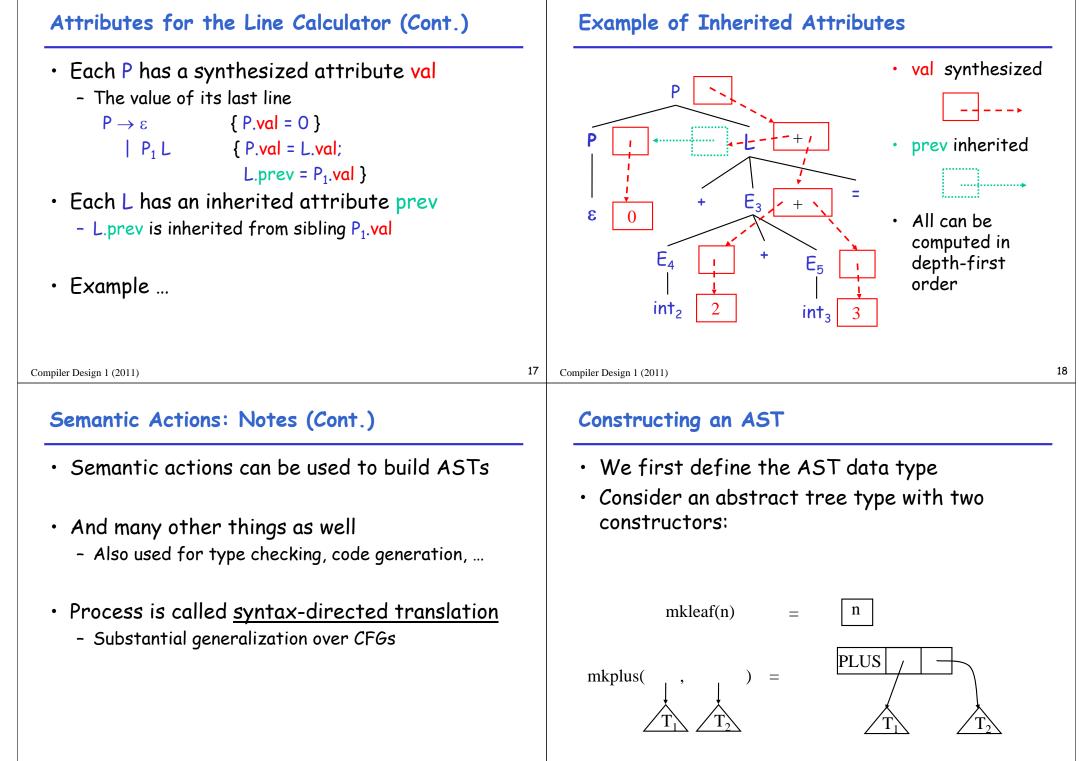
Example of Parse Tree

E PLUS Traces the operation of the parser PLUS E • Captures the nesting structure • But too much info int₅ 3 5 F - Parentheses - Single-successor nodes Also captures the nesting structure • But abstracts from the concrete syntax \mapsto more compact and easier to use int₂ int₃ • An important data structure in a compiler 5 Compiler Design 1 (2011) Compiler Design 1 (2011) Semantic Actions Semantic Actions: An Example This is what we'll use to construct ASTs • Consider the grammar $E \rightarrow int | E + E | (E)$ Each grammar symbol may have <u>attributes</u> ٠ For each symbol X define an attribute X.val - An attribute is a property of a programming - For terminals, val is the associated lexeme language construct - For non-terminals, val is the expression's value - For terminal symbols (lexical tokens) attributes can (which is computed from values of subexpressions) be calculated by the lexer • We annotate the grammar with actions: Each production may have an <u>action</u> $E \rightarrow int$ { E.val = int.val } - Written as: $X \rightarrow Y_1 \dots Y_n = \{ action \} \}$ $| E_1 + E_2$ { E.val = E_1 .val + E_2 .val } - That can refer to or compute symbol attributes $\{ (E_1) \} \{ E.val = E_1.val \}$

Example of Abstract Syntax Tree

Semantic Actions: An Example (Cont.) Semantic Actions: Dependencies Semantic actions specify a system of equations • String: 5 + (2 + 3)- Order of executing the actions is not specified • Tokens: $int_5 + ('int_2 + int_3)'$ • Example: Productions Equations E_3 , val = E_4 , val + E_5 , val E.val = E_1 .val + E_2 .val $E \rightarrow E_1 + E_2$ - Must compute E_4 .val and E_5 .val before E_3 .val $E_1 \rightarrow int_5$ E_1 .val = int₅.val = 5 - We say that E_3 , val depends on E_4 , val and E_5 , val $E_2 \rightarrow (E_3)$ E_2 .val = E_3 .val $E_3 \rightarrow E_4 + E_5$ $E_3.val = E_4.val + E_5.val$ • The parser must find the order of evaluation $E_4 \rightarrow int_2$ E_4 .val = int₂.val = 2 $E_5 \rightarrow int_3$ $E_5.val = int_3.val = 3$ 9 Compiler Design 1 (2011) Compiler Design 1 (2011) **Dependency** Graph **Evaluating Attributes** • An attribute must be computed after all its • Each node labeled with F a non-terminal E has successors in the dependency graph have been one slot for its val computed attribute E_2 - In the previous example attributes can be Note the dependencies computed bottom-up int₅ E₃ + \ • Such an order exists when there are no cycles - Cyclically defined attributes are not legal E₄ E int₂ int,

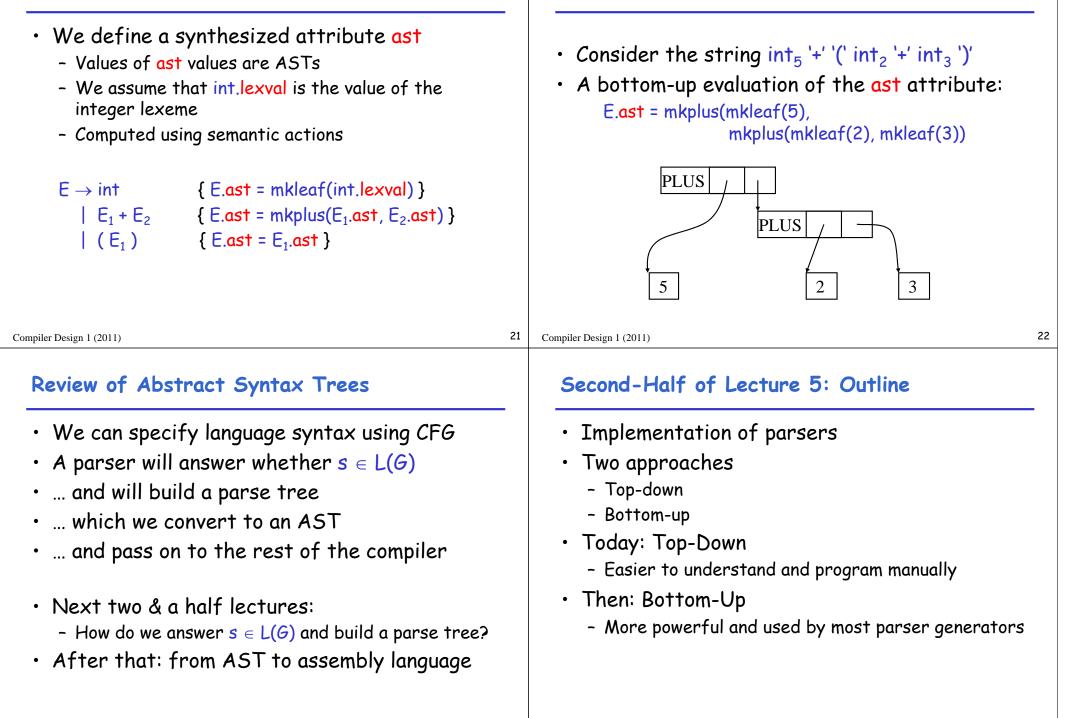
 Semantic Actions: Notes (Cont.) Synthesized attributes Calculated from attributes of descendents in the parse tree E.val is a synthesized attribute Can always be calculated in a bottom-up order Grammars with only synthesized attributes are called <u>S-attributed</u> grammars Most frequent kinds of grammars 	 Inherited Attributes Another kind of attributes Calculated from attributes of the parent node(s) and/or siblings in the parse tree Example: a line calculator 		
Compiler Design 1 (2011) 13 A Line Calculator	Compiler Design 1 (2011) Attributes for the Line Calculator	14	
 Each line contains an expression E → int E + E Each line is terminated with the = sign L → E = + E = In the second form, the value of evaluation of the previous line is used as starting value A program is a sequence of lines P → ε PL 	 Each E has a synthesized attribute val Calculated as before Each L has a synthesized attribute val L→E = {L.val = E.val } I + E = {L.val = E.val + L.prev } We need the value of the previous line We use an inherited attribute L.prev 		



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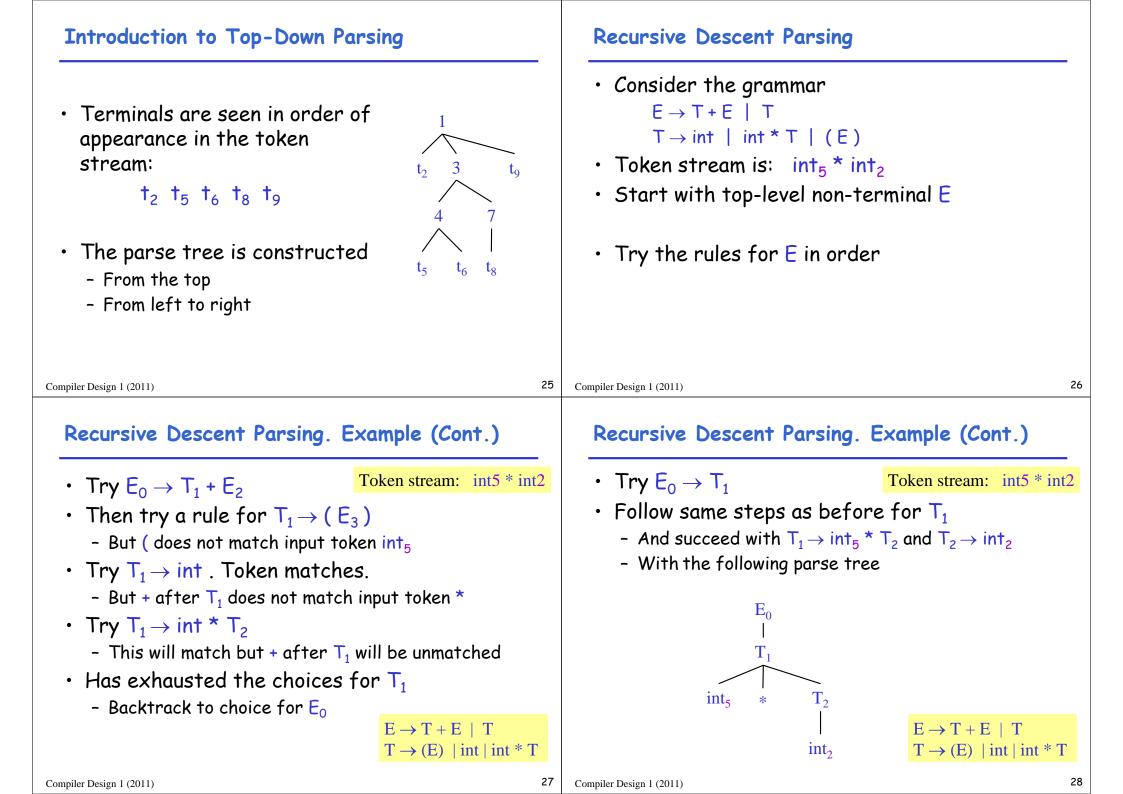
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Constructing a Parse Tree



Parse Tree Example

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Recursive Descent Parsing. Notes.	When Recursive Descent Does Not Work
 Easy to implement by hand Somewhat inefficient (due to backtracking) But does not always work 	 Consider a production S → S a bool S₁() { return S() && term(a); } bool S() { return S₁(); } S() will get into an infinite loop A <u>left-recursive grammar</u> has a non-terminal S S →⁺ Sα for some α Recursive descent does not work in such cases
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Elimination of Left Recursion	More Elimination of Left-Recursion
 Consider the left-recursive grammar S → S α β S generates all strings starting with a β and followed by any number of α's The grammar can be rewritten using right- recursion S → β S' S' → α S' ε 	• In general $S \rightarrow S \alpha_1 \mid \mid S \alpha_n \mid \beta_1 \mid \mid \beta_m$ • All strings derived from S start with one of $\beta_1,,\beta_m$ and continue with several instances of $\alpha_1,,\alpha_n$ • Rewrite as $S \rightarrow \beta_1 S' \mid \mid \beta_m S'$ $S' \rightarrow \alpha_1 S' \mid \mid \alpha_n S' \mid \varepsilon$

General Left Recursion	Summary of Recursive Descent		
• The grammar $S \rightarrow A \alpha \mid \delta$ $A \rightarrow S \beta$ is also left-recursive because $S \rightarrow^{+} S \beta \alpha$	 Simple and general parsing strategy Left-recursion must be eliminated first but that can be done automatically Unpopular because of backtracking Thought to be too inefficient 		
 This left-recursion can also be eliminated See a Compilers book for a general algorithm 	 In practice, backtracking is eliminated by restricting the grammar 		
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Predictive Parsers	LL(1) Languages		
 Like recursive-descent but parser can "predict" which production to use By looking at the next few tokens No backtracking Predictive parsers accept LL(k) grammars L means "left-to-right" scan of input L means "leftmost derivation" k means "predict based on k tokens of lookahead" In practice, LL(1) is used 	 In recursive-descent, for each non-terminal and input token there may be a choice of production LL(1) means that for each non-terminal and token there is only one production Can be specified via 2D tables One dimension for current non-terminal to expand One dimension for next token A table entry contains one production 		

Predictive Parsing and Left Factoring						Left-Factoring Example		
 Recall the grammar for arithmetic expressions E→T+E T T→(E) int int * T Hard to predict because For T two productions start with int For E it is not clear how to predict A grammar must be <u>left-factored</u> before it is used for predictive parsing 					ic exp	• Recall the grammar $E \rightarrow T + E \mid T$ $T \rightarrow (E) \mid \text{ int } \mid \text{ int } * T$ • Factor out common prefixes of productions $E \rightarrow T X$ $X \rightarrow + E \mid \varepsilon$ $T \rightarrow (E) \mid \text{ int } Y$ $Y \rightarrow * T \mid \varepsilon$		
ompiler Design			Svempl			37	Compiler Design 1 (2011)	
LL(1) Parsing Table Example• Left-factored grammar $E \rightarrow T X$ $X \rightarrow + E \mid \epsilon$ $T \rightarrow (E) \mid int Y$ $Y \rightarrow * T \mid \epsilon$ • The LL(1) parsing table:					·Ε ε	 LL(1) Parsing Table Example (Cont.) Consider the [E, int] entry "When current non-terminal is E and next input is int, use production E → T X This production can generate an int in the first place Consider the [Y+] entry 		
• The	$T \rightarrow (E)$	int Y		¥ → *	3 Τ		int, use production $E \rightarrow T X$ - This production can generate an int in the first	
	$T \rightarrow (E)$ e LL(1) po	int Y		(3 T)	\$	 int, use production E → T X This production can generate an int in the first place Consider the [Y,+] entry "When current non-terminal is Y and current token 	
• The	$T \rightarrow (E)$ e LL(1) po	int y arsing to	ıble:	$\begin{array}{c} Y \rightarrow * \\ \hline \\ (\\ T \\ \\ (E) \end{array}$	3 T () 3		 int, use production E → T X This production can generate an int in the first place Consider the [Y,+] entry 	

LL(1)	Parsing	Tables:	Errors
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 LL(1) Parsing Tables: Errors Blank entries indicate error situations Consider the [E,*] entry "There is no way to derive a string starting with * from non-terminal E" 		Using Parsing Tables			
		 Method similar to recursive descent, except For each non-terminal S We look at the next token a And chose the production shown at [S,a] We use a stack to keep track of pending non-terminals We reject when we encounter an error state We accept when we encounter end-of-input 			
ompiler Design 1 (2011)	41	Compiler Design 1 (2011)			
LL(1) Parsing Algorithm		LL(1) Parsi	ng Example		
<pre>initialize stack = <s \$=""> and next repeat case stack of</s></pre>		<u>Stack</u> E \$ T X \$ int Y X \$ Y X \$ * T X \$ T X \$ int Y X \$ Y X \$ Y X \$ X \$ \$	<u>Input</u> int * int \$ int * int \$ int * int \$ * int \$ * int \$ int \$ int \$ \$ \$	$\begin{array}{c} Action \\ T X \\ int Y \\ terminal \\ * T \\ terminal \\ int Y \\ terminal \\ \epsilon \\ \epsilon \\ ACCEPT \\ \hline \hline int & * + () \\ \hline E TX & TX \\ \hline x & + E \\ \end{array}$	
ompiler Design 1 (2011)	43	Compiler Design 1 (2011)		T int Y (Ε) y * T ε ε	

Constructing Parsing Tables	Constructing Parsing Tables (Cont.)		
 LL(1) languages are those defined by a parsing table for the LL(1) algorithm No table entry can be multiply defined We want to generate parsing tables from CFG 	 If A → α, where in the line of A we place α? In the column of t where t can start a string derived from α α →* t β We say that t ∈ First(α) In the column of t if α is ε and t can follow an A S →* β A t δ We say t ∈ Follow(A) 		
Compiler Design 1 (2011) 45	Compiler Design 1 (2011) 46		
Computing First Sets $ \frac{\text{Definition}}{\text{First}(X) = \{ + X \to^* t\alpha \} \cup \{ \epsilon X \to^* \epsilon \} \\ \frac{\text{Algorithm sketch}}{1. \text{ First}(t) = \{ + \} \\ 2. \epsilon \in \text{First}(X) \text{ if } X \to \epsilon \text{ is a production} \\ 3. \epsilon \in \text{First}(X) \text{ if } X \to A_1 \dots A_n \\ \text{and } \epsilon \in \text{First}(A_i) \text{ for each } 1 \le i \le n \\ 4. \text{First}(\alpha) \subseteq \text{First}(X) \text{ if } X \to A_1 \dots A_n \\ \text{and } \epsilon \in \text{First}(A_i) \text{ for each } 1 \le i \le n \\ \end{cases} $	First Sets: Example • Recall the grammar $E \rightarrow TX$ $X \rightarrow + E \mid \varepsilon$ $T \rightarrow (E) \mid int Y$ $Y \rightarrow * T \mid \varepsilon$ • First sets First(() = {(} First()) = {)} First(+) = {+} First(*) = {*} First(int) = { int } First(int) = { int , (} First(E) = { int, (} First(X) = {+, ε }		
Compiler Design 1 (2011) 47	$First(Y) = \{*, \varepsilon\}$ Compiler Design 1 (2011)		

Computing Follow Sats

Computing Follow Sets	Computing Follow Sets (Cont.)		
 Definition Follow(X) = { t S →[*] β X t δ } Intuition - If X → A B then First(B) ⊆ Follow(A) and Follow(X) ⊆ Follow(B) Also if B →[*] ε then Follow(X) ⊆ Follow(A) If S is the start symbol then \$ ∈ Follow(S) 	Algorithm sketch1. $\$ \in Follow(S)$ 2. First(β) - { ϵ } \subseteq Follow(X) For each production $A \rightarrow \alpha \times \beta$ 3. Follow(A) \subseteq Follow(X) For each production $A \rightarrow \alpha \times \beta$ where $\epsilon \in First(\beta)$		
Compiler Design 1 (2011) 49 Follow Sets: Example	Compiler Design 1 (2011) 50 Constructing LL(1) Parsing Tables		
• Recall the grammar $E \rightarrow T X$ $X \rightarrow + E \mid \epsilon$	Construct a parsing table T for CFG G		
$T \to (E) \mid int Y \qquad Y \to *T \mid \varepsilon$ • Follow sets Follow(+) = { int, (} Follow(*) = { int, (} Follow(() = { int, (} Follow(E) = {), \$ } Follow(X) = { \$, \$ } Follow(T) = { +, \$, \$ } Follow() = { +, \$, \$ Follow(Y) = { +, \$, \$ } Follow(int) = { *, +, \$, \$ }	• For each production $A \rightarrow \alpha$ in G do: - For each terminal $t \in First(\alpha)$ do $\cdot T[A, t] = \alpha$ - If $\varepsilon \in First(\alpha)$, for each $t \in Follow(A)$ do $\cdot T[A, t] = \alpha$ - If $\varepsilon \in First(\alpha)$ and $\$ \in Follow(A)$ do $\cdot T[A, \$] = \alpha$		

Notes on LL(1) Parsing Tables		Review	
 If any entry is multiply defined then G is not LL(1) 	-	 For some grammars there is a simple parsing strategy 	_
 If G is ambiguous If G is left recursive 		Predictive parsing	
 If G is not left-factored <u>And in other cases as well</u> 		 Next time: a more powerful parsing strategy 	
 Most programming language grammars are not LL(1) 			
 There are tools that build LL(1) tables 			
ompiler Design 1 (2011)	53	Compiler Design 1 (2011)	54