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**Torsten Söderström: Discrete-Time Stochastic Systems**, second edition, Springer-Verlag, 2002.

Below, pa.b denotes page a, line b (pa.b- denotes page a, line b from below).

### Errata

p26 A more unambiguous formulation of Exercise 2.4 is the following.

Let  $v$  and  $e$  be two random vectors of zero mean that are jointly Gaussian. Let  $e$  have a positive definite covariance matrix. Show that there exist a unique matrix  $B$  and a random vector  $w$  such that

- (i)  $v = Be + w$
- (ii)  $e$  and  $w$  are independent

p114 A more unambiguous formulation of Exercise 4.1 is the following.

Give a simple example of two stochastic processes, say  $y_1(t)$  and  $y_2(t)$ , that fulfil the following:

- (i) The first and all second order moments are the same, that is

$$\begin{aligned}\mathbf{E} y_1(t) &= \mathbf{E} y_2(t) \\ \mathbf{E} y_1(t)y_1(t+\tau) &= \mathbf{E} y_2(t)y_2(t+\tau) \quad \text{all } \tau\end{aligned}$$

- (ii) The realizations (outcomes) of  $y_1(t)$  and  $y_2(t)$  look significantly different. From a measured data record  $y(1), y(2), \dots, y(N)$ , it should be possible to tell if  $y_1(t)$  or  $y_2(t)$  is observed.

p134 A more unambiguous formulation of Exercise 5.1 is the following.

Let  $x \sim \mathbf{N}(m_x, R_x)$  and  $e \sim \mathbf{N}(0, R_e)$  be independent Gaussian random vectors. Suppose one observes

$$y = Cx + e .$$

- (a) Determine the mean square optimal estimate of  $x$  based on the observation  $y$ .
- (b) What is the covariance matrix of the estimation error? What is the covariance matrix of the estimate?

265.2 This line is missing and should read:  
to let the correct model in operation have a probability close to one.

265.4- Read

$$\hat{x}(t) \triangleq \mathbf{E} [x(t)|Y^t] = \int x(t)p(x(t)|Y^t) \, dx(t)$$

268.5- Read

$$\hat{x}(t) = \mathbf{E} [x(t)|Y^{t-1}]$$

268.4-, 3-, 1- Replace  $N$  by  $M$ , totally 6 times.

p367.6 Read (c)  $p_{\eta|\xi=x}(y) = \gamma(y; 2 - 2\rho + 2\rho x, 4 - 4\rho^2)$

p368.10 The answer to Exercise 4.19, last line should read

$$H^{(2)} = \begin{pmatrix} H^{(1)} & I \end{pmatrix}, \quad R_2^{(2)} = 0.$$

p368.8- The answer to Exercise 5.1 should read:

- (a)  $(x|y) \sim \mathbf{N}(\hat{x}, P)$ ,  $\hat{x} = m_x + R_x C^T (C R_x C^T + R_e)^{-1} (y - C m_x)$ .
- (b)  $\text{cov}(x - \hat{x}) = P = R_x - R_x C^T (C R_x C^T + R_e)^{-1} C R_x$ ,  
 $\text{cov}(\hat{x}) = \text{cov}(x) - P = R_x - P = R_x C^T (C R_x C^T + R_e)^{-1} C R_x$ .