

## Defining Loops With Dominators

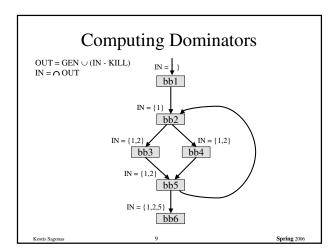
- Concept of *dominator* 
   Node n <u>dominates</u> a node m if all paths from start node to m go through n
- If  $d_1$  and  $d_2$  both dominate m, then either
  - $d_1$  dominates  $d_2$ , or
  - d<sub>2</sub> dominates d<sub>1</sub> (but not both look at path from start)
- *Immediate dominator* of m last dominator of m on any path from start node

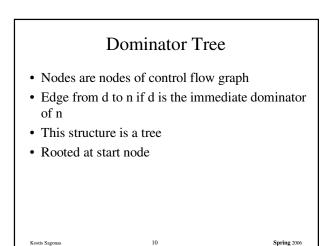
### Dominator Problem Formulation • A cross product of the lattice for each basic block: - Lattice per basic block T = dominated $\downarrow \pm = not dominated$ • Flow direction: Forward Flow • Dataflow Equations: - GEN = { $b_k | b_k$ is the current basic block } - KILL = { } - OUT = GEN $\cup$ (IN - KILL)

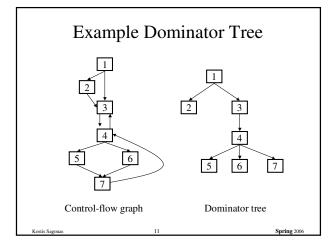
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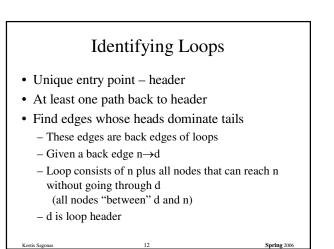
 $-IN = \cap OUT$ 

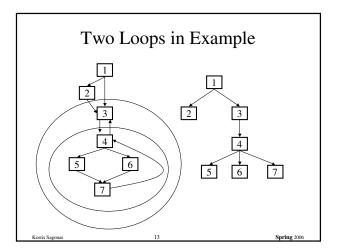
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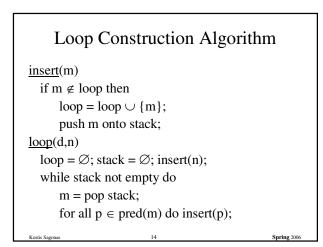


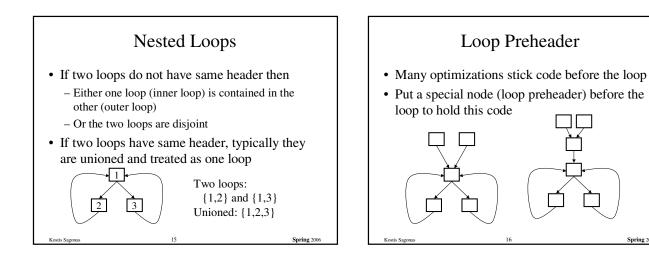


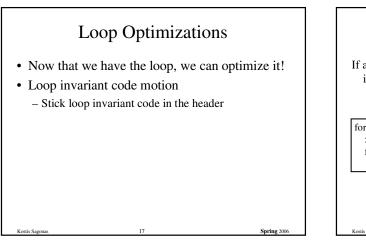


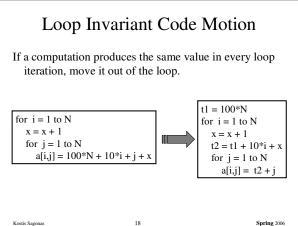












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## Detecting Loop Invariant Code

- A statement is *loop-invariant* if operands are
  - Constant,
  - Have all reaching definitions outside loop, or
  - Have exactly one reaching definition, and that definition comes from an invariant statement
- Concept of exit node of loop – node with successors outside loop

### Loop Invariant Code Detection Algorithm

for all statements in loop

if operands are constant or have all reaching definitions outside loop, mark statement as invariant

do

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for all statements in loop not already marked invariant

if operands are constant, have all reaching definitions outside loop, or have exactly one reaching definition from invariant statement

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then mark statement as invariant

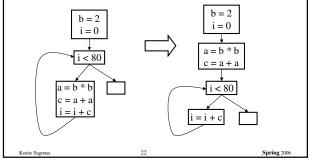
until there are no more invariant statements

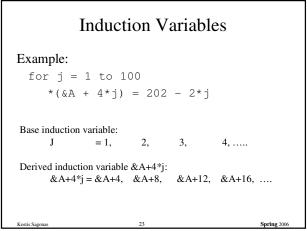
# Loop Invariant Code Motion

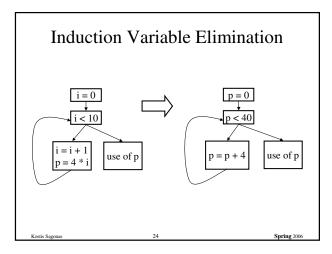
- Conditions for moving a statement s: x = y+z into loop header:
  - The node containing s dominates all exit nodes of loop
    - If it does not, some use after loop might get wrong value
    - Alternate condition: definition of x from s reaches no use outside loop (but moving s may increase run time)
  - No other statement in loop assigns to x
    - If one does, assignments might get reordered
  - No use of x in loop is reached by definition other than s
    - If one is, movement may change value read by use
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### Order of Statements in Preheader

Preserve data dependences from original program (can use order in which discovered by algorithm)







# What are induction variables?

- x is an *induction variable* of a loop L if
  - variable changes its value on every loop iteration
  - the value is a function of number of iterations of the loop
- In many programs, this function is often a linear function

Example: for loop index variable j, function d + c\*j

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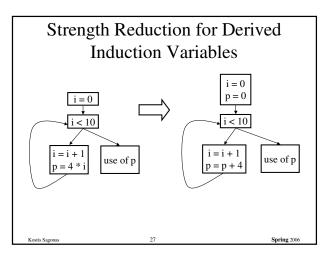
## What is an Induction Variable?

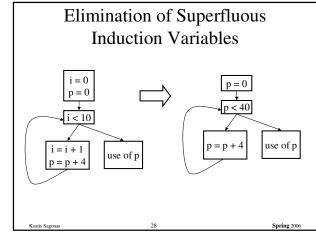
- Base induction variable
  - Only assignments in loop are of form  $i = i \pm c$
- Derived induction variables
  - Value is a linear function of a base induction variable
  - Within loop,  $j = c^*i + d$ , where i is a base induction variable

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 Very common in array index expressions – an access to a[i] produces code like p = a + 4\*i



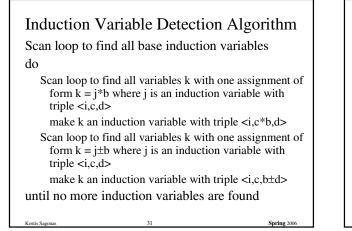


# Three Algorithms

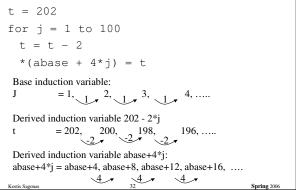
- Detection of induction variables
  - Find base induction variables
  - Each base induction variable has a family of derived induction variables, each of which is a linear function of base induction variable
- Strength reduction for derived induction variables
- Elimination of superfluous induction variables

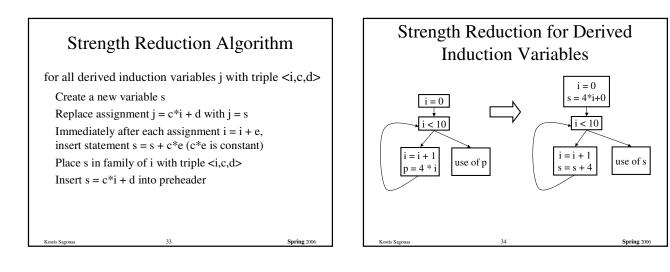
# Output of Induction Variable Detection Algorithm

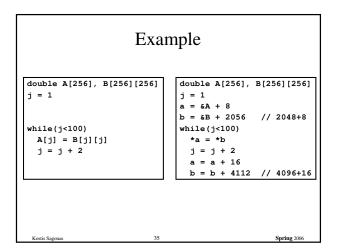
- Set of induction variables
  - base induction variables
  - derived induction variables
- For each induction variable j, a triple <i,c,d>
  - i is a base induction variable
  - the value of j is i\*c+d
  - j belongs to family of i

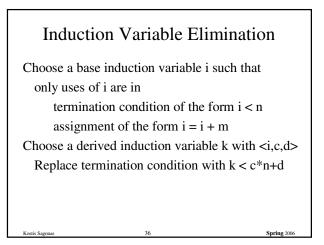


#### Strength Reduction









# Induction Variable Wrap-up

There is lots more to induction variables

- more general classes of induction variables
- more general transformations involving induction variables

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# Compiler Optimization Summary

- Wide range of analyses and optimizations
- Dataflow analyses and corresponding optimizations
  - reaching definitions, constant propagation
    live variable analysis, dead code elimination
- Induction variable analyses and loop optimizations
  - Strength reduction
  - Induction variable elimination
  - Important because lots of time is spent in loops

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